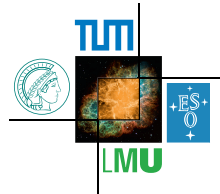


# Model-dependent Flavour Constraints on New Physics

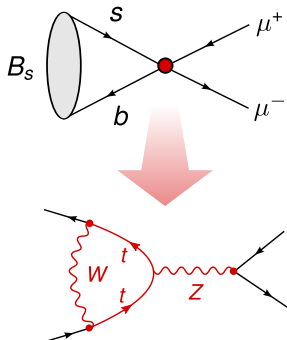
Presented by David M. Straub

Junior Research Group “New Physics”  
Excellence Cluster Universe, Munich



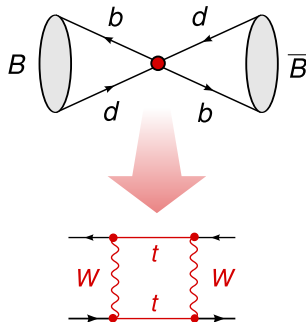
# Flavour-changing neutral currents

$\Delta F = 1$ : rare decays



$$\mathcal{H}_{\text{eff}} \supset \frac{\delta}{\Lambda^2} \mathcal{O}$$

$\Delta F = 2$ : meson-antimeson mixing

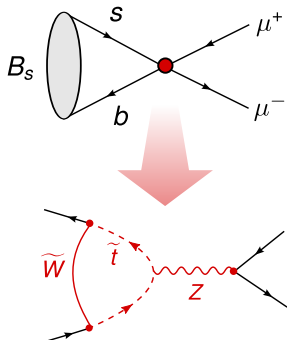


$$\mathcal{H}_{\text{eff}} \supset \frac{\delta^2}{\Lambda^2} \mathcal{O}$$

Typical new physics model: scale  $\Lambda$ , flavour changing parameter  $\delta$

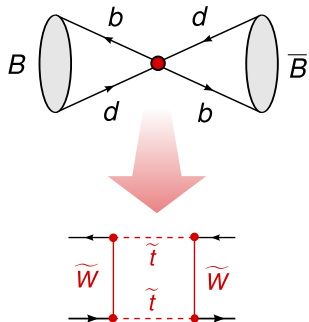
# Flavour-changing neutral currents

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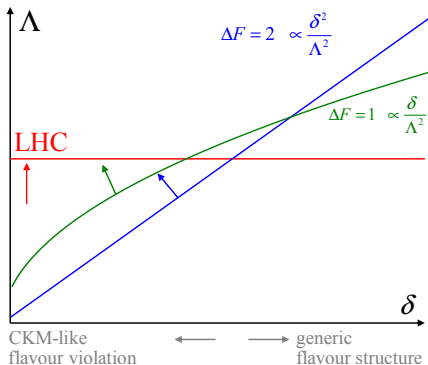
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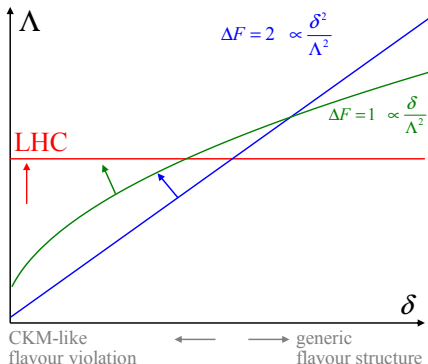
Typical new physics model: scale  $\Lambda$ , flavour changing parameter  $\delta$

# Flavour vs. collider bounds on the new physics scale $\Lambda$



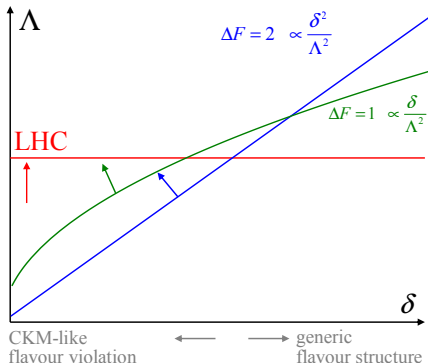
- Collider physics: directly probes  $\Lambda$  – limited by  $\sqrt{s}$

# Flavour vs. collider bounds on the new physics scale $\Lambda$



- ▶ Meson-antimeson mixing: can probe the highest scales  
 But only small number of observables sensitive to NP ( $\Delta M, \phi$ )

# Flavour vs. collider bounds on the new physics scale $\Lambda$



- Rare decays: much more observables, more sensitive to “small” flavour violation at “natural” scales

# Outline

- 1 Introduction
- 2 Flavour vs. collider bounds on Supersymmetry
  - Meson mixing in natural SUSY
  - $B_s \rightarrow \mu^+ \mu^-$
- 3 Rare decays in Composite Higgs models

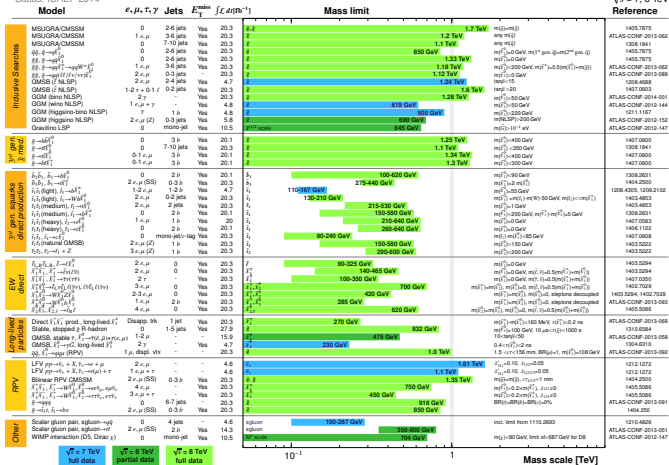
# Direct searches: no sign of SUSY!

## ATLAS SUSY Searches\* - 95% CL Lower Limits

Status: ICHP 2014

ATLAS Preliminary

$\sqrt{s} = 7, 8 \text{ TeV}$

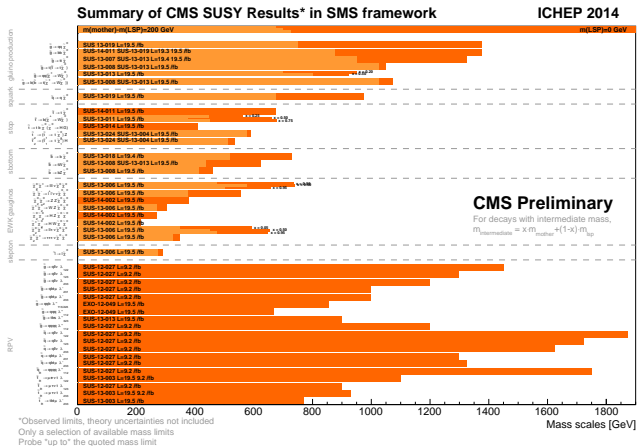


\*Only a selection of the available mass limits on new states or phenomena is shown. All limits quoted are observed minus 1 $\sigma$  theoretical signal cross section uncertainty.

NB: bounds on 3rd gen' quarks and EWinos generally weakest

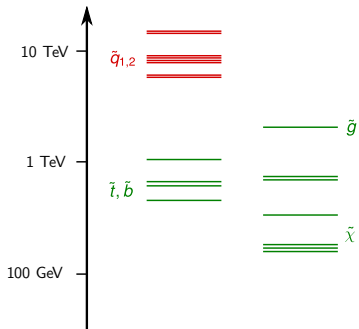


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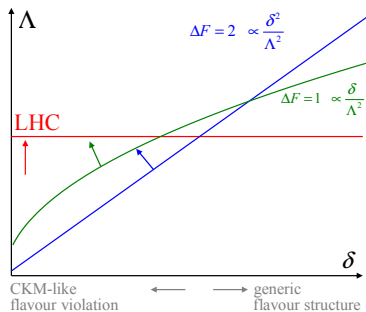
NB: bounds on 3rd gen' quarks and EWinos generally weakest

# A natural SUSY spectrum, summer 2014



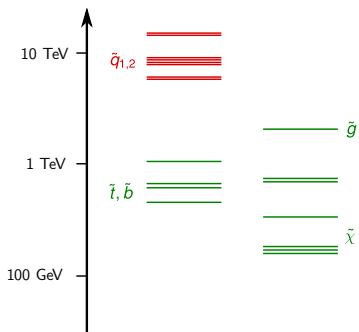
- ▶ Strong LHC bounds on 1st/2nd generation squarks
- ▶ Light 3rd generation squarks to solve hierarchy problem

# Are flavour bounds competitive with collider bounds?



Considering the case where flavour bounds are weakest: CKM-like flavour violation

## Natural SUSY & $U(2)^3$



- ▶ Strong LHC bounds on 1st/2nd generation squarks
- ▶ Light 3rd generation squarks to solve hierarchy problem

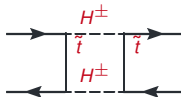
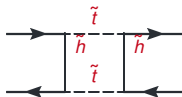
Natural SUSY with split generations + CKM-like flavour violation: approximate, minimally broken  $U(2)^3$  flavour symmetry (“split MFV”)

[Barbieri et al. 1105.2296]

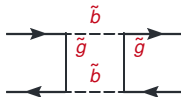
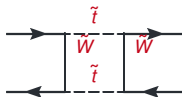
# Meson mixing in SUSY $U(2)^3$

Two classes of contributions

- ▶ Higgsino and ch. Higgs contributions are MFV-like

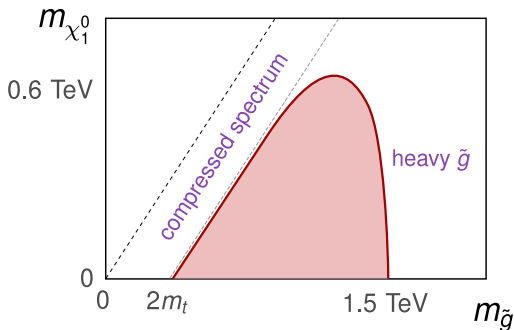


- ▶ Wino and gluino contributions can induce a new phase in  $B/B_s$  mixing



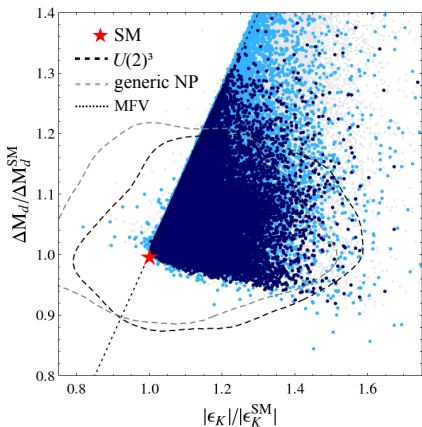
## Sparticle mass bounds in natural SUSY

Typically, two ways for sparticles to evade LHC bounds. E.g.,  $\tilde{g} \rightarrow t\bar{t}\chi_1^0$ :



- ▶ heavy spectrum: contribution to flavour observables will be suppressed
- ▶ compressed spectrum: potentially large contribution to flavour obs.
- ▶ similarly for  $\tilde{t}$ ,  $\tilde{b}$

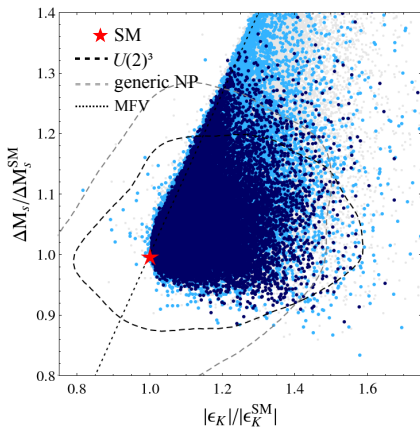
## Numerical results for $\Delta F = 2$ observables



- ▶ All blue points fulfill collider bounds
- ▶ Dashed lines:  $\Delta F = 2$  constraints (black:  $U(2)^3$ , gray: generic)
- ▶ Direct bounds almost as constraining as flavour, except for **compressed spectra**

[Barbieri et al. 1402.6677]

## Numerical results for $\Delta F = 2$ observables

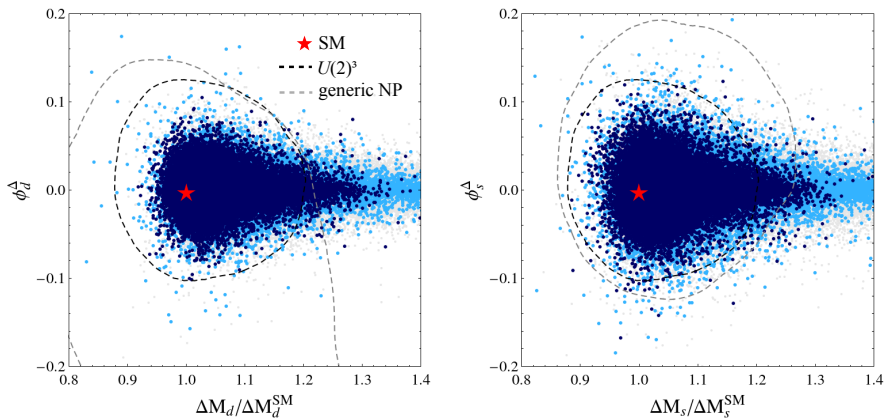


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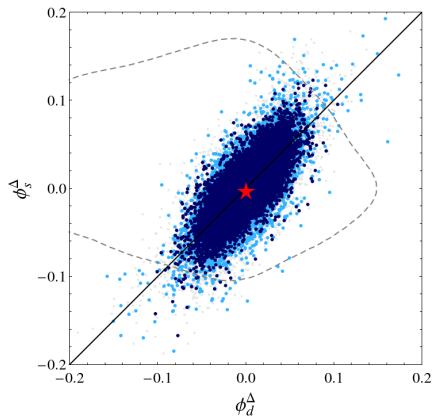
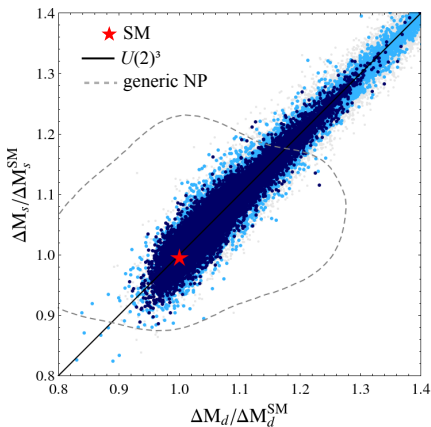


## Numerical results for $\Delta F = 2$ observables



- $B_{S,d}$  mixing phase at most 0.1, whether **compressed** or not

## Numerical results for $\Delta F = 2$ observables



- ▶  $U(2)^3$  symmetry relates  $B_s$  and  $B_d$  mixing

## 1 Introduction

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- $B_s \rightarrow \mu^+ \mu^-$

## 3 Rare decays in Composite Higgs models

## $B_s \rightarrow \mu^+ \mu^-$ beyond the SM

$$\mathcal{H}_{\text{eff}} = -\frac{4 G_F}{\sqrt{2}} \frac{e^2}{16\pi^2} V_{tb} V_{ts}^* \sum_i C_i O_i + C'_i O'_i + \text{h.c.}$$

$$O_{10}^{(l)} = (\bar{s} \gamma_\mu P_{L(R)} b) (\bar{l} \gamma^\mu \gamma_5 l)$$

$$O_S^{(l)} = (\bar{s} P_{R(L)} b) (\bar{l} P_{L(R)} l)$$

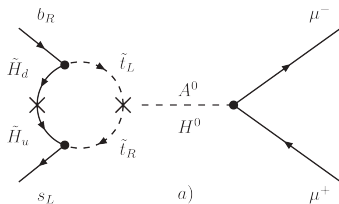
$$\text{BR}(B_s \rightarrow \mu^+ \mu^-) \propto |S|^2 + |P|^2$$

$$S = \frac{m_b}{2} (C_S - C'_S) \quad P = \frac{m_b}{2} (-C_S - C'_S) + m_\mu C_{10}$$

Scalar contributions lift the helicity suppression!

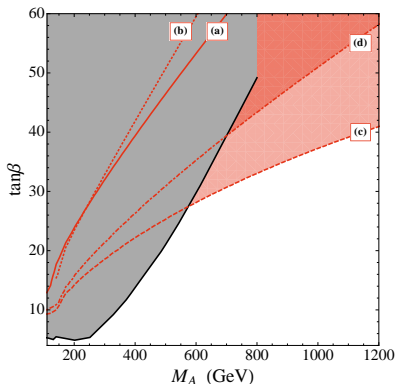
# Scalar operators in the MSSM

Even with Minimal Flavour Violation,  $(\tan \beta)^3$  enhanced contribution to  $C_S$



$$C_S^{\tilde{H}} \propto \frac{\tan \beta^3}{M_A^2} \frac{A_t \mu}{m_{\tilde{t}}^2} f_{\tilde{H}} \left( \frac{|\mu|^2}{m_{\tilde{t}}^2} \right)$$

# Complementarity with Higgs searches



$$m_{\tilde{q}} = 2 \text{ TeV}, 6M_1 = 3M_2 = M_3 = 1.5 \text{ TeV}$$

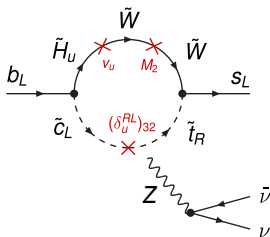
Scenario	(a)	(b)	(c)	(d)	(e)
$\mu$ [TeV]	1	4	-1.5	1	-1.5
$\text{sign}(A_t)$	+	+	+	-	-

- ▶ Large  $\tan \beta$  + light Higgs spectrum disfavoured
- ▶ Direct Higgs searches more constraining for  $\tan \beta \lesssim 25$
- ▶ Milder bounds for  $\mu A_t > 0$  (destructive interference with SM)

[Altmannshofer et al. 1211.1976]

## New physics in Z penguins: $C_{10}$ in SUSY

- ▶ If there are no sizable scalar operators,  $B_s \rightarrow \mu^+ \mu^-$  allows a clean measurement of Z penguin!
- ▶ Complementary to  $B \rightarrow K^{(*)} \mu^+ \mu^-$  and  $B \rightarrow K^{(*)} \nu \bar{\nu}$
- ▶ Only way to get sizable  $C_{10}$  in SUSY: Z penguin with chargino loop



- ▶ Up to 25% effect in BR

## 1 Introduction

## 2 Flavour vs. collider bounds on Supersymmetry

- Meson mixing in natural SUSY
- $B_s \rightarrow \mu^+ \mu^-$

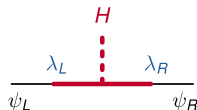
## 3 Rare decays in Composite Higgs models



## Composite Higgs & partial compositeness

- ▶ Solving the hierarchy problem without SUSY: the Higgs is composite
- ▶ Successful theory of flavour requires quarks to be partially composite

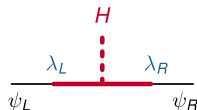
$$\mathcal{L} \supset \lambda_L \bar{\psi}_L \mathcal{O}_R + \lambda_R \bar{\psi}_R \mathcal{O}_L$$



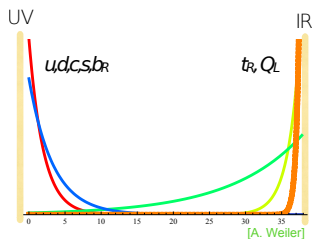
## Composite Higgs & partial compositeness

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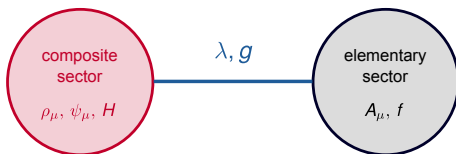
Related by AdS/CFT to models with a warped extra dimension



# The two-site picture

[Contino et al. hep-ph/0612180]

A simple 4D theory realizing the partial compositeness paradigm



$$\mathcal{L}_S = -\bar{Q}_L m_Q Q_R - \bar{U}_L m_U U_R - \bar{D}_L m_D D_R \\ + \bar{Q}_L \mathcal{H} Y_U U_R + \bar{Q}_L \mathcal{H} Y_D D_R + \text{h.c.}$$

$$\mathcal{L}_{\text{mix}} = \lambda_L \bar{q}_L Q_R + \lambda_{Ru} \bar{U}_L U_R + \lambda_{Rd} \bar{D}_L D_R$$

$$q^{\text{phys}} = c_L q + s_L Q \quad \frac{s_L}{c_L} = \frac{\lambda_L}{m_Q} \quad m_{q^{\text{phys}}} = \frac{v}{\sqrt{2}} Y s_L s_R \quad \text{etc.}$$

## Flavour anarchy

- ▶ Structureless (“anarchic”) composite Yukawas
- ▶ Hierarchies in quark masses and mixing generated by hierarchical composite-elementary mixing

$$y_u^i = S_{Li} Y_{U*} S_{Rui}$$

$$S_{L3} \gg S_{L2} \gg S_{L1}$$

$$S_{Ru3} \gg S_{Ru2} \gg S_{Ru1}$$

$$V_{CKM}^{ij} \sim \frac{S_{Li}}{S_{Lj}}$$

## Anarchic FCNCs



Relation between c.-el. mixings and quark masses & CKM leads to a suppression of FCNCs (“RS-GIM”):

$$s_{L_i}^2 s_{L_j}^2 \sim (V_{3i}^* V_{3j})^2 s_{L_t}^2$$

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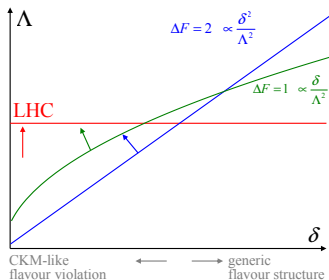
$$s_{Li}^2 s_{Lj}^2 \sim (V_{3i}^* V_{3j})^2 s_{Lt}^2$$

**but** also RR and LR FCNCs

$$s_{Li}^2 s_{Rj}^2 \sim y_{di} y_{dj}$$

Operator  $(\bar{s}_R d_L)(\bar{s}_L d_R)$  leads to a bound of order **14 TeV** from  $\epsilon_K$ !

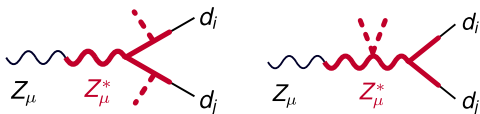
## Flavour symmetries for partial compositeness



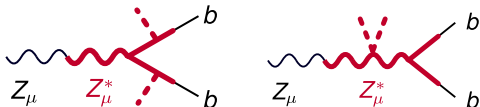
- ▶ flavour anarchy  $\Rightarrow$  high compositeness scale required by  $\Delta F = 2$
- ▶ Introducing a flavour symmetry, comp. scale can be sub-TeV:  $U(2)^3$  symmetry minimally broken by composite-elementary mixings  
[Barbieri et al. 1203.4218, Barbieri et al. 1211.5085]
- ▶ Potentially interesting effects in  $\Delta F = 1$

## Z penguins from partial compositeness

After EWSB, composite-elementary mixing leads to correlated tree-level contributions to flavour-changing  $Z$  couplings ...



... and  $Z \rightarrow b\bar{b}$



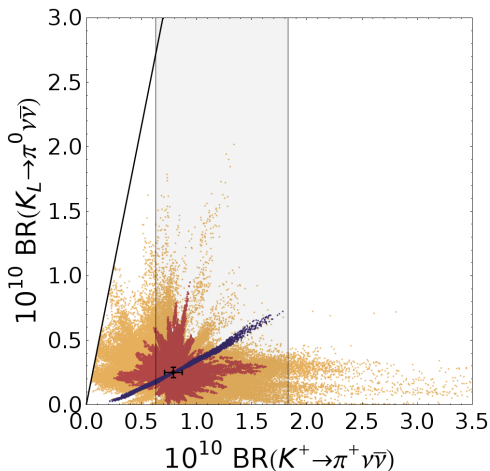


## Numerical analysis of $Z$ penguins in 3 models

- ▶ Two choices for the fermion content (representations of  $SU(2)_L \times SU(2)_R \times U(1)_X$ ) to protect  $T$  parameter and  $Z \rightarrow b\bar{b}$ 
  - ▶  $(2, 2)_{2/3} + (2, 2)_{-1/3} + (1, 1)_{2/3} + (1, 1)_{-1/3}$  (“**bidoublet** model”)
  - ▶  $(2, 2)_{2/3} + (1, 3)_{2/3} + (3, 1)_{2/3}$  (“**triplet** model”)
- ▶ Two choices for the flavour structure
  - ▶ flavour **anarchy**
  - ▶  $U(2)^3$  flavour symmetry

see [[Barbieri et al. 1203.4218](#), [Barbieri et al. 1211.5085](#), [Straub 1302.4651](#)] and ref. therein

$$K^+ \rightarrow \pi^+ \nu \bar{\nu} \text{ vs. } K_L \rightarrow \pi^0 \nu \bar{\nu}$$



triplet + anarchy

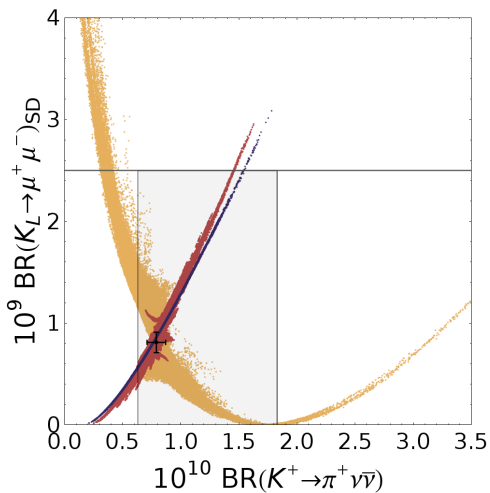
bidoublet + anarchy

bidoublet +  $U(2)^3$

- ▶ Visible effects in both modes
- ▶  $U(2)^3$ : aligned in phase with the SM

[Straub 1302.4651]

$$K^+ \rightarrow \pi^+ \nu \bar{\nu} \text{ vs. } K_L \rightarrow \mu^+ \mu^-$$



triplet + anarchy

bidoublet + anarchy

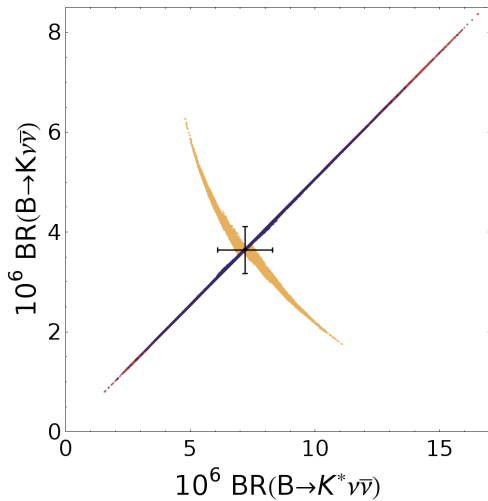
bidoublet +  $U(2)^3$

▶ triplet: RH coupling

▶ bidoublet: LH coupling

[Straub 1302.4651]

# $B \rightarrow K\nu\bar{\nu}$ vs. $B \rightarrow K^*\nu\bar{\nu}$



triplet + anarchy

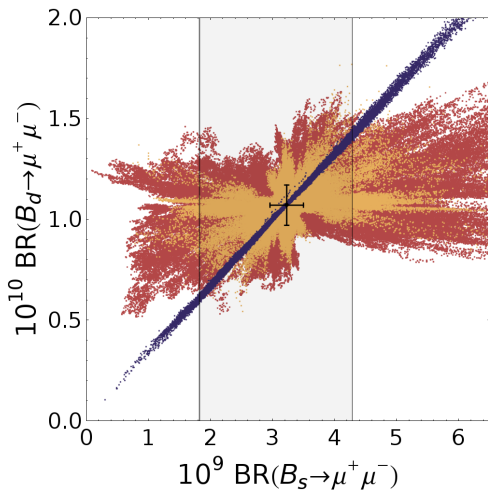
bidoublet + anarchy

bidoublet +  $U(2)^3$

- ▶ triplet: RH coupling
- ▶ bidoublet: LH coupling

[Straub 1302.4651]

# $B_s \rightarrow \mu\mu$ vs. $B_d \rightarrow \mu\mu$

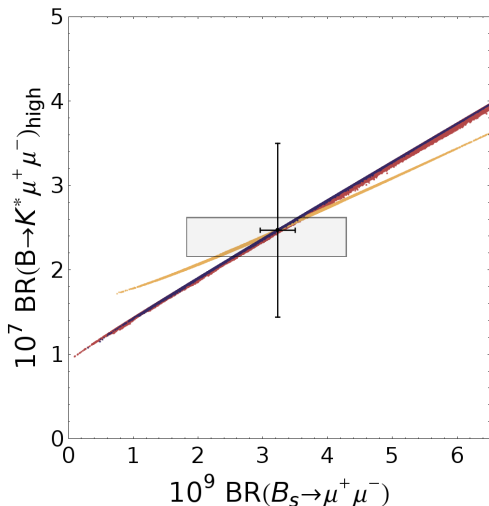


triplet + anarchy  
bidoublet + anarchy  
bidoublet +  $U(2)^3$

- ▶ LHCb **starts** to probe the models
- ▶ MFV-like  $B_d \leftrightarrow B_s$  correlation in  $U(2)^3$

[Straub 1302.4651]

# $B_s \rightarrow \mu\mu$ vs. $B \rightarrow K^* \mu\mu$



triplet + anarchy

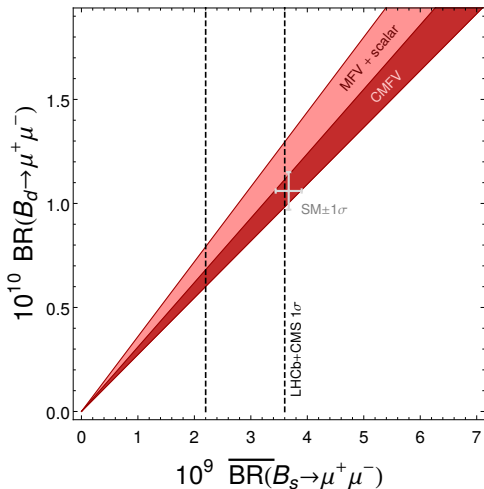
bidoublet + anarchy

bidoublet +  $U(2)^3$

- Correlation due to protection of LH or RH  $bsZ$  coupling

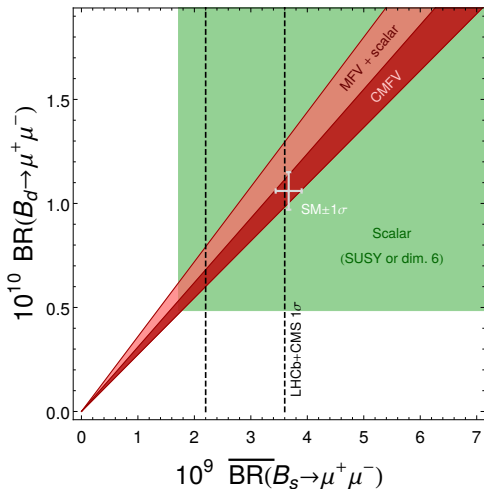
[Straub 1302.4651]

## Model-independently: $B_s \rightarrow \mu\mu$ vs. $B_d \rightarrow \mu\mu$



- ▶  $B_s \rightarrow \mu\mu$  vs.  $B_d \rightarrow \mu\mu$ : powerful test of Minimal Flavour Violation

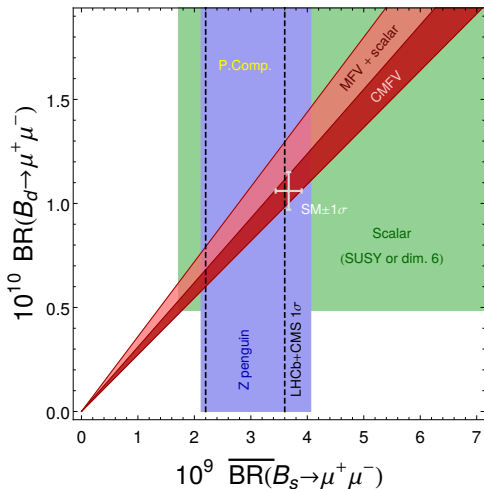
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- ▶  $B_s \rightarrow \mu\mu$  vs.  $B_d \rightarrow \mu\mu$ : powerful test of Minimal Flavour Violation
- ▶ Beyond MFV: scalar operators (e.g. SUSY) unconstrained by other processes

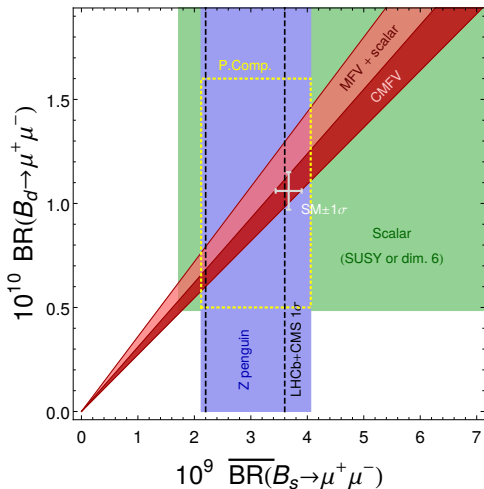


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# Conclusions

Natural SUSY with minimally broken  $U(2)^3$  flavour symmetry:

- ▶ flavour & collider bounds complementary
- ▶ flavour bounds stronger for compressed spectrum
- ▶  $\phi_s$  small, but potentially around the corner

Rare decays in composite Higgs models:

- ▶ Flavour symmetry desirable to suppress CPV in kaon mixing
- ▶ Pattern of effects in rare decays could allow to distinguish models

# Backup

## Two ways to CKM-like flavour violation

### Minimal Flavour Violation (MFV) [D'Ambrosio et al. hep-ph/0207036]

- ▶  $U(3)_{Q_L} \times U(3)_{U_R} \times U(3)_{D_R}$  flavour symmetry
- ▶ broken minimally by Yukawa couplings  $Y_u, Y_d$
- ▶ all FCNC amplitudes suppressed by same CKM factors as in SM
- ▶ perfect correlation between  $s \leftrightarrow d, b \leftrightarrow s, b \leftrightarrow d$

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- ▶  $U(3)_{Q_L} \times U(3)_{U_R} \times U(3)_{D_R}$  flavour symmetry
- ▶ broken minimally by Yukawa couplings  $Y_u, Y_d$
- ▶ all FCNC amplitudes suppressed by same CKM factors as in SM
- ▶ perfect correlation between  $s \leftrightarrow d, b \leftrightarrow s, b \leftrightarrow d$

### “Minimal $U(2)^3$ ” [Barbieri et al. 1105.2296]

- ▶  $U(2)_{Q_L} \times U(2)_{U_R} \times U(2)_{D_R}$  flavour symmetry
- ▶ broken minimally by three spurions
- ▶ all FCNC amplitudes suppressed by same CKM factors as in SM
- ▶ perfect correlation **only** between  $b \leftrightarrow s$  and  $b \leftrightarrow d$ , **new phases**

## Meson-antimeson mixing

Mixing amplitudes  $M_{12}$  in the  $K$ ,  $B_d$ ,  $B_s$  systems can be written as

$$M_{12}^K = (M_{12}^K)_{\text{SM}} (1 + h_K e^{2i\sigma_K})$$

$$M_{12}^d = (M_{12}^d)_{\text{SM}} (1 + h_d e^{2i\sigma_d})$$

$$M_{12}^s = (M_{12}^s)_{\text{SM}} (1 + h_s e^{2i\sigma_s})$$

- ▶ **MFV**:  $\sigma_{K,d,s} = 0$  and  $h_{K,d,s} \equiv h$
- ▶  **$U(2)^3$** :  $\sigma_K = 0$ ,  $h_K, h_{d,s} \equiv h_B$   $\sigma_{d,s} \equiv \sigma_B$

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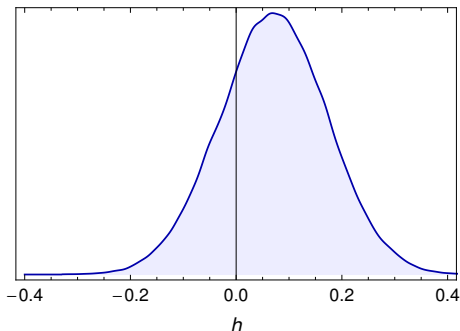
- ▶ **MFV**:  $\sigma_{K,d,s} = 0$  and  $h_{K,d,s} \equiv h$
- ▶  **$U(2)^3$** :  $\sigma_K = 0$ ,  $h_K, h_{d,s} \equiv h_B$ ,  $\sigma_{d,s} \equiv \sigma_B$

What are the allowed sizes of  $h$  or  $h_B, h_K, \sigma_B$ ?



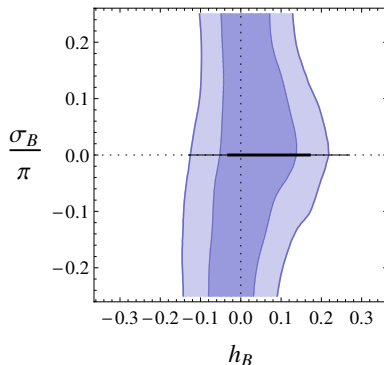
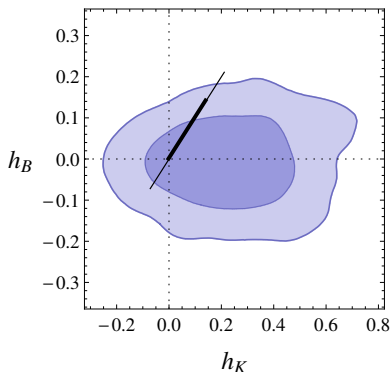
## Meson-antimeson mixing in MFV

Global fit to  $\Delta M_d$ ,  $\Delta M_s$ ,  $\phi_s$ ,  $S_{\psi K_S}$ ,  $\epsilon_K$ ,  $\gamma$ ,  $|V_{ud}|$ ,  $|V_{us}|$ ,  $|V_{cb}|$ ,  $|V_{ub}|$ :



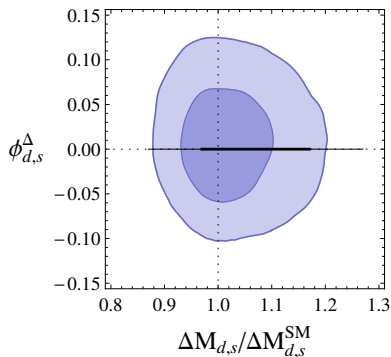
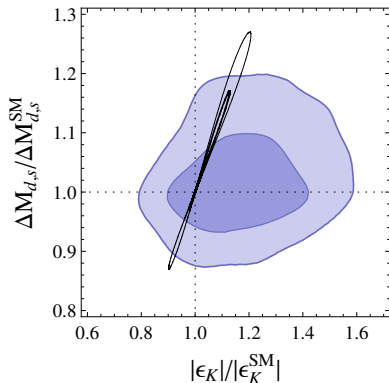
- ▶ MFV-like modification of mixing amplitudes constrained to  $\pm 20\%$

# Meson-antimeson mixing in $U(2)^3$



- ▶ Slight preference for a positive contribution to  $h_K$  ( $\epsilon_K$ )
- ▶ Modification in  $B/B_s$  mixing phase small due to  $\phi_s$  constraint

# Meson-antimeson mixing in $U(2)^3$



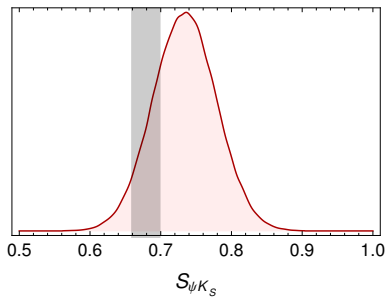
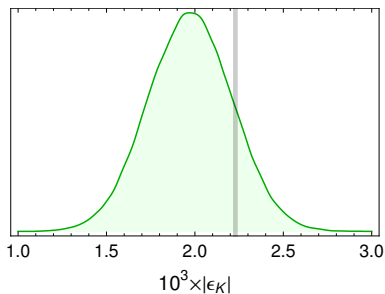
- ▶ Slight preference for a positive contribution to  $h_K$  ( $\epsilon_K$ )
- ▶ Modification in  $B/B_s$  mixing phase small due to  $\phi_s$  constraint

## $\epsilon_K$ vs. $S_{\psi K_S}$

- ▶ There is a long-standing **tension** in the SM CKM fit between  $\epsilon_K$ ,  $S_{\psi K_S} = \sin 2\beta$  and  $\Delta M_d/\Delta M_s$  that can be solved in  $U(2)^3$ , **not** in MFV
- ▶ What is the status of this tension?

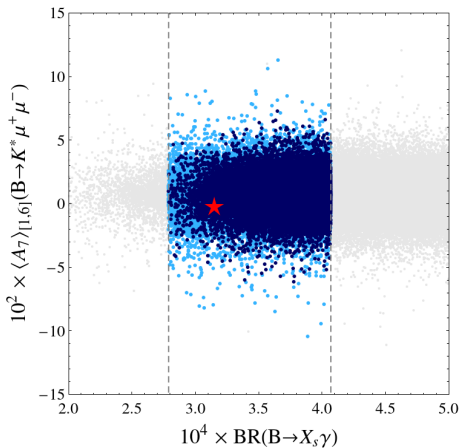
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- ▶ What is the status of this tension?



- ▶ Significance of “tension” down to  **$1.1\sigma$**
- ▶ Main reason: lattice bag parameter  $\hat{B}_K$  moved up; theory uncertainty on  $\eta_{cc}$  increased

# $\Delta F = 1$ in SUSY $U(2)^3$



NB:  $\tan \beta \leq 5$

## (Pseudo-)scalar operators in the MSSM *without* MFV

$$C_S^{\tilde{W}} \propto (\delta_d^{LL})_{32} \frac{\tan \beta^3 M_2 \mu}{M_A^2 m_{\tilde{t}}^2} f_{\tilde{W}} \left( \frac{|\mu|^2}{m_{\tilde{t}}^2}, \frac{|M_2|^2}{m_{\tilde{t}}^2} \right)$$

$$C_S^{\tilde{g}} \propto -(\delta_d^{LL})_{32} \frac{\tan \beta^3 M_3 \mu}{M_A^2 m_{\tilde{b}}^2} f_{\tilde{g}} \left( \frac{|M_3|^2}{m_{\tilde{b}}^2} \right)$$

$$C_S^{\prime \tilde{g}} \propto -(\delta_d^{RR})_{32} \frac{\tan \beta^3 M_3 \mu}{M_A^2 m_{\tilde{b}}^2} f_{\tilde{g}} \left( \frac{|M_3|^2}{m_{\tilde{b}}^2} \right)$$

- ▶  $(\delta_d^{LL})_{32}$  strongly constrained by  $b \rightarrow s\gamma$
- ▶  $(\delta_d^{RR})_{32}$  constrained by  $b \rightarrow s\gamma$  and  $\Delta M_s$

## CHM: pattern of flavour-changing Z couplings

- ▶ triplet model:  $P_{LR}$  forbids  $g_L^{ij}$
- ▶ bidoublet model:  $P_C$  forbids  $g_R^{ij}$
- ▶  $U(2)^3$  forbids  $g_R^{ij}$

		$K$		$B_{d,s}$		$D$	
		$L$	$R$	$L$	$R$	$L$	$R$
$\mathbb{A}$	triplet		$\mathbb{C}$		$\mathbb{C}$	$\mathbb{C}$	
	bidoublet	$\mathbb{C}$		$\mathbb{C}$		$\mathbb{C}$	
$U(2)_{LC}^3$	triplet					$\mathbb{R}$	
	bidoublet	$\mathbb{R}$		$\mathbb{C}$		$\mathbb{R}$	