

SMEFT Studies Using Machine Learning

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Based on : Felipe F. Freitas, CKK, Veronica Sanz, arXiv: 1902.05803 [hep-ph]

$$pp \rightarrow H(\rightarrow bb) + Z(\rightarrow ll)$$

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SM Effective Field Theory(SMEFT)

$$\mathcal{L}^{d=6} = \mathcal{L}_{SM} + \sum_i \frac{C_i}{\Lambda^2} \mathcal{O}_i$$

$$\begin{aligned} \mathcal{L}_{\text{SMEFT}}^{\text{SILH}} \supset & \frac{\bar{c}_W}{m_W^2} \frac{ig}{2} \left(H^\dagger \sigma^a \overleftrightarrow{D}^\mu H \right) D^\nu W_{\mu\nu}^a + \frac{\bar{c}_B}{m_W^2} \frac{ig'}{2} \left(H^\dagger \overleftrightarrow{D}^\mu H \right) \partial^\nu B_{\mu\nu} + \frac{\bar{c}_T}{v^2} \frac{1}{2} \left(H^\dagger \overleftrightarrow{D}_\mu H \right)^2 \\ & + \frac{\bar{c}_{ll}}{v^2} (\bar{L} \gamma_\mu L) (\bar{L} \gamma^\mu L) + \frac{\bar{c}_{He}}{v^2} (i H^\dagger \overleftrightarrow{D}_\mu H) (\bar{e}_R \gamma^\mu e_R) + \frac{\bar{c}_{Hu}}{v^2} (i H^\dagger \overleftrightarrow{D}_\mu H) (\bar{u}_R \gamma^\mu u_R) \\ & + \frac{\bar{c}_{Hd}}{v^2} (i H^\dagger \overleftrightarrow{D}_\mu H) (\bar{d}_R \gamma^\mu d_R) + \frac{\bar{c}'_{Hq}}{v^2} (i H^\dagger \sigma^a \overleftrightarrow{D}_\mu H) (\bar{Q}_L \sigma^a \gamma^\mu Q_L) \\ & + \frac{\bar{c}_{Hq}}{v^2} (i H^\dagger \overleftrightarrow{D}_\mu H) (\bar{Q}_L \gamma^\mu Q_L) + \frac{\bar{c}_{HW}}{m_W^2} ig (D^\mu H)^\dagger \sigma^a (D^\nu H) W_{\mu\nu}^a + \frac{\bar{c}_{HB}}{m_W^2} ig' (D^\mu H)^\dagger (D^\nu H) B_{\mu\nu} \\ & + \frac{\bar{c}_{3W}}{m_W^2} g^3 \epsilon_{abc} W_\mu^a W_\nu^b W^{\rho\mu}_c + \frac{\bar{c}_g}{m_W^2} g_s^2 |H|^2 G_{\mu\nu}^A G^{A\mu\nu} + \frac{\bar{c}_\gamma}{m_W^2} g'^2 |H|^2 B_{\mu\nu} B^{\mu\nu} \\ & + \frac{\bar{c}_H}{v^2} \frac{1}{2} (\partial^\mu |H|^2)^2 + \sum_{f=e,u,d} \frac{\bar{c}_f}{v^2} y_f |H|^2 \bar{F}_L H^{(c)} f_R \\ & + \frac{\bar{c}_{3G}}{m_W^2} g_s^3 f_{ABC} G_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu} + \frac{\bar{c}_{uG}}{m_W^2} g_s y_u \bar{Q}_L H^{(c)} \sigma^{\mu\nu} \lambda_A u_R G_{\mu\nu}^A \end{aligned}$$

SMEFT : Global Analysis

- Precision electroweak data, LHC Run 1 & 2 data (Higgs production, pair of gauge bosons)

Observable	Measurement	Ref.	SM Prediction	Ref.
Γ_Z [GeV]	2.4952 ± 0.0023	[41]	2.4943 ± 0.0005	[40]
σ_{had}^0 [nb]	41.540 ± 0.037	[41]	41.488 ± 0.006	[40]
R_ℓ^0	20.767 ± 0.025	[41]	20.752 ± 0.005	[40]
$A_{\text{FB}}^{0,\ell}$	0.0171 ± 0.0010	[41]	0.01622 ± 0.00009	[120]
$\mathcal{A}_\ell(P_\tau)$	0.1465 ± 0.0033	[41]	0.1470 ± 0.0004	[120]
$\mathcal{A}_\ell(\text{SLD})$	0.1513 ± 0.0021	[41]	0.1470 ± 0.0004	[120]
R_b^0	0.021629 ± 0.00066	[41]	0.2158 ± 0.00015	[40]
R_c^0	0.1721 ± 0.0030	[41]	0.17223 ± 0.00005	[40]
$A_{\text{FB}}^{0,b}$	0.0992 ± 0.0016	[41]	0.1031 ± 0.0003	[120]
$A_{\text{FB}}^{0,c}$	0.0707 ± 0.0035	[41]	0.0736 ± 0.0002	[120]
$\mathcal{A}_b$	0.923 ± 0.020	[41]	0.9347	[120]
$\mathcal{A}_c$	0.670 ± 0.027	[41]	0.6678 ± 0.0002	[120]
M_W [GeV]	80.387 ± 0.016	[42]	80.361 ± 0.006	[120]
M_W [GeV]	80.370 ± 0.019	[100]	80.361 ± 0.006	[120]

LEP data
+
WW LEP2 data
+
 M_W Tevatron

Production	Decay	Signal Strength	Production	Decay	Signal Strength
ggF	$\gamma\gamma$	$1.10^{+0.23}_{-0.22}$	Wh	$\tau\tau$	-1.4 ± 1.4
ggF	ZZ	$1.13^{+0.34}_{-0.31}$	Wh	bb	1.0 ± 0.5
ggF	WW	0.84 ± 0.17	Zh	$\gamma\gamma$	$0.5^{+3.0}_{-2.5}$
ggF	$\tau\tau$	1.0 ± 0.6	Zh	WW	$5.9^{+2.6}_{-2.2}$
VBF	$\gamma\gamma$	1.3 ± 0.5	Zh	$\tau\tau$	$2.2^{+2.2}_{-1.8}$
VBF	ZZ	$0.1^{+1.1}_{-0.6}$	Zh	bb	0.4 ± 0.4
VBF	WW	1.2 ± 0.4	tth	$\gamma\gamma$	$2.2^{+1.6}_{-1.3}$
VBF	$\tau\tau$	1.3 ± 0.4	tth	WW	$5.0^{+1.8}_{-1.7}$
Wh	$\gamma\gamma$	$0.5^{+1.3}_{-1.2}$	tth	$\tau\tau$	$-1.9^{+3.7}_{-3.3}$
Wh	WW	$1.6^{+1.2}_{-1.0}$	tth	bb	1.1 ± 1.0
pp	$Z\gamma$	$2.7^{+4.6}_{-4.5}$	pp	$\mu\mu$	0.1 ± 2.5

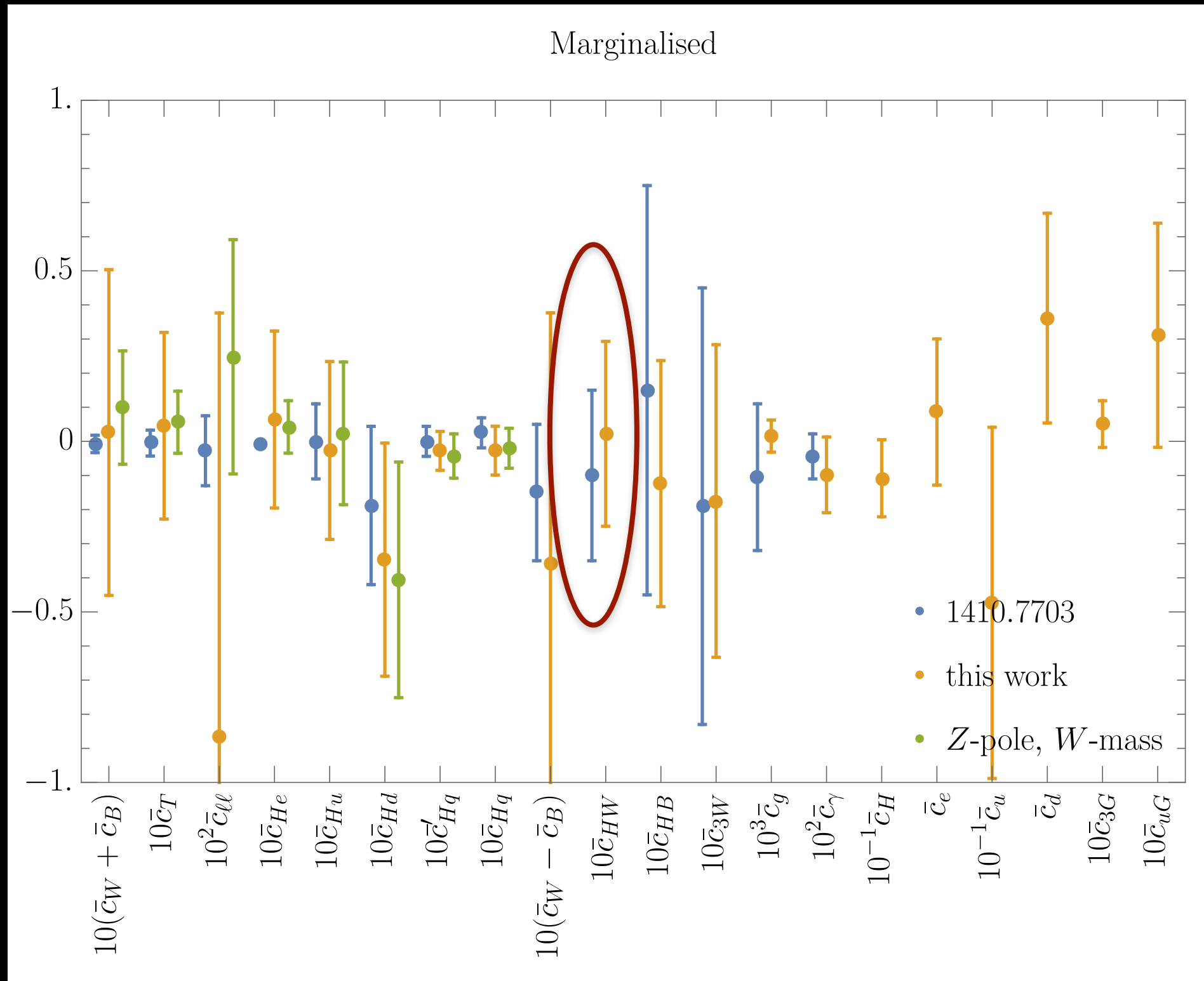
(Early) Run 2 data

+

STXS

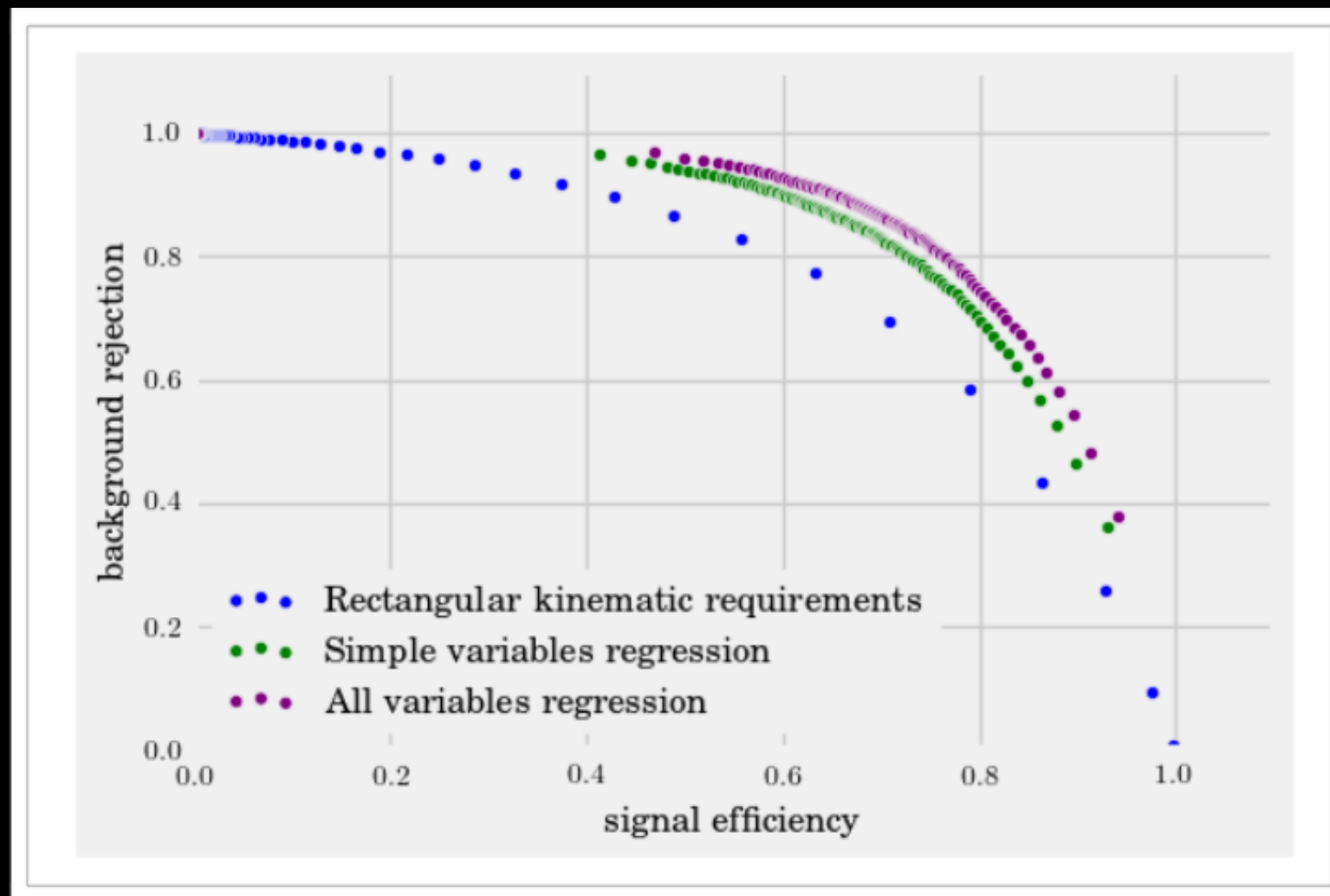
← Run 1 data

	Production	Decay	Sig. Stren.		Production	Decay	Sig. Stren.
[102]	1-jet, $p_T > 450$	$b\bar{b}$	$2.3^{+1.8}_{-1.6}$	[110]	pp	$\mu\mu$	-0.1 ± 1.5
[103]	Zh	$b\bar{b}$	0.9 ± 0.5	[111]	Zh	$b\bar{b}$	$1.12^{+0.50}_{-0.45}$
[103]	Wh	$b\bar{b}$	1.7 ± 0.7	[111]	Wh	$b\bar{b}$	$1.35^{+0.68}_{-0.59}$
[104]	$t\bar{t}h, \geq 1\ell$	$b\bar{b}$	0.72 ± 0.45	[112]	$t\bar{t}h$	$b\bar{b}$	$0.84^{+0.64}_{-0.61}$
[105]	$t\bar{t}h$	$1\ell + 2\tau_h$	$-1.52^{+1.76}_{-1.72}$	[113]	$t\bar{t}h$	$2\ell os + 1\tau_h$	$1.7^{+2.1}_{-1.9}$
[105]	$t\bar{t}h$	$2\ell ss + 1\tau_h$	$0.94^{+0.80}_{-0.67}$	[113]	$t\bar{t}h$	$1\ell + 2\tau_h$	$-0.6^{+1.6}_{-1.5}$
[105]	$t\bar{t}h$	$3\ell + 1\tau_h$	$1.34^{+1.42}_{-1.07}$	[113]	$t\bar{t}h$	$3\ell + 1\tau_h$	$1.6^{+1.8}_{-1.3}$
[105]	$t\bar{t}h$	$2\ell ss$	$1.61^{+0.58}_{-0.51}$	[113]	$t\bar{t}h$	$2\ell ss + 1\tau_h$	$3.5^{+1.7}_{-1.3}$
[105]	$t\bar{t}h$	3ℓ	$0.82^{+0.77}_{-0.71}$	[113]	$t\bar{t}h$	3ℓ	$1.8^{+0.9}_{-0.7}$
[105]	$t\bar{t}h$	4ℓ	$0.9^{+2.3}_{-1.6}$	[113]	$t\bar{t}h$	$2\ell ss$	$1.5^{+0.7}_{-0.6}$
[106]	0-jet DF	WW	$1.30^{+0.24}_{-0.23}$	[114]	ggF	WW	$1.21^{+0.22}_{-0.21}$
[106]	1-jet DF	WW	$1.29^{+0.32}_{-0.27}$	[114]	VBF	WW	$0.62^{+0.37}_{-0.36}$
[106]	2-jet DF	WW	$0.82^{+0.54}_{-0.50}$	[115]	$B(h \rightarrow \gamma\gamma) / B(h \rightarrow 4\ell)$		$0.69^{+0.15}_{-0.13}$
[106]	VBF 2-jet	WW	$0.72^{+0.44}_{-0.41}$	[115]	0-jet	4ℓ	$1.07^{+0.27}_{-0.25}$
[106]	Vh 2-jet	WW	$3.92^{+1.32}_{-1.17}$	[115]	1-jet, $p_T < 60$	4ℓ	$0.67^{+0.72}_{-0.68}$
[106]	Wh 3-lep	WW	$2.23^{+1.76}_{-1.53}$	[115]	1-jet, $p_T \in (60, 120)$	4ℓ	$1.00^{+0.63}_{-0.55}$
[107]	ggF	$\gamma\gamma$	$1.10^{+0.20}_{-0.18}$	[115]	1-jet, $p_T \in (120, 200)$	4ℓ	$2.1^{+1.5}_{-1.3}$
[107]	VBF	$\gamma\gamma$	$0.8^{+0.6}_{-0.5}$	[115]	2-jet	4ℓ	$2.2^{+1.1}_{-1.0}$
[107]	$t\bar{t}h$	$\gamma\gamma$	$2.2^{+0.9}_{-0.8}$	[115]	“BSM-like”	4ℓ	$2.3^{+1.2}_{-1.0}$
[107]	Vh	$\gamma\gamma$	$2.4^{+1.1}_{-1.0}$	[115]	VBF, $p_T < 200$	4ℓ	$2.14^{+0.94}_{-0.77}$
[108]	ggF	4ℓ	$1.20^{+0.22}_{-0.21}$	[115]	Vh lep	4ℓ	$0.3^{+1.3}_{-1.2}$
[109]	0-jet	$\tau\tau$	0.84 ± 0.89	[115]	$t\bar{t}h$	4ℓ	$0.51^{+0.86}_{-0.70}$
[109]	boosted	$\tau\tau$	$1.17^{+0.47}_{-0.40}$	[116]	Wh	WW	$3.2^{+4.4}_{-4.2}$
[109]	VBF	$\tau\tau$	$1.11^{+0.34}_{-0.35}$				
[106]	Zh 4-lep	WW	$0.77^{+1.49}_{-1.20}$				



Why Machine Learning is required for HEP analyses?

Classification between signal and background process



Need to quickly identify subtle effects in multidimensional distributions

P. Mehta et al., [arXiv:1803.08823\[physics.comp-ph\]](https://arxiv.org/abs/1803.08823)

SMEFT analyses using ML

VBF channel (not a reality yet)

J. Brehmer, K. Cranmer, G. Louppe and J Pavez,
Phys. Rev. Lett. 121 (2018) 111801, Phys. Rev. D 98 (2018) 052004

VH channel (data available)

Felipe F. Freitas, CKK, Veronica Sanz, arXiv: 1902.05803 [hep-ph]

**Our approach is to use a better algorithm to
analyse the data which is available now**

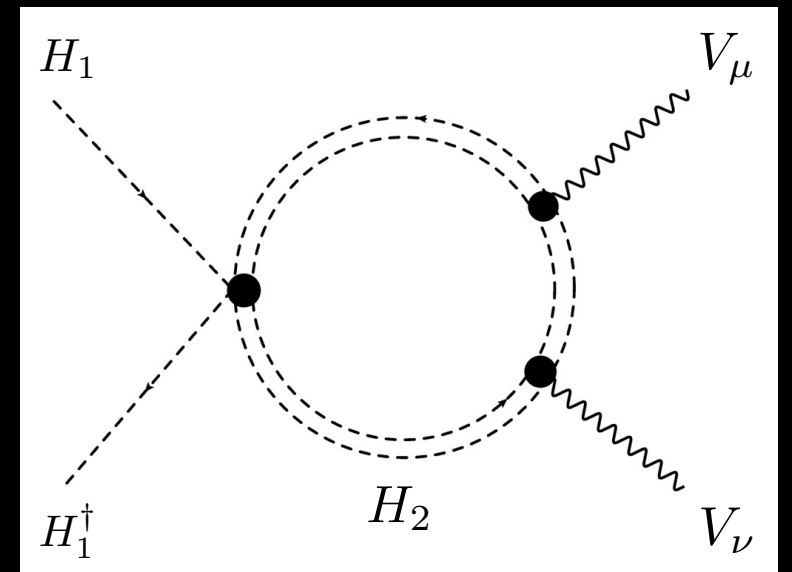
More subtle kinematic signatures

Higgs EFT via VH channel

Generic EFT effect

$$\eta_{\mu\nu} g m_V \Rightarrow \eta_{\mu\nu} g m_V - \frac{2 g c_{HW}}{m_W} p_\mu^V p_\nu^V + \dots$$

$$\mathcal{L}_{SM} \Rightarrow \mathcal{L}_{SM} + \frac{2igc_{HW}}{m_W^2} [D^\mu H^\dagger T_{2k} D^\nu H] W_{\mu\nu}^k + \dots$$



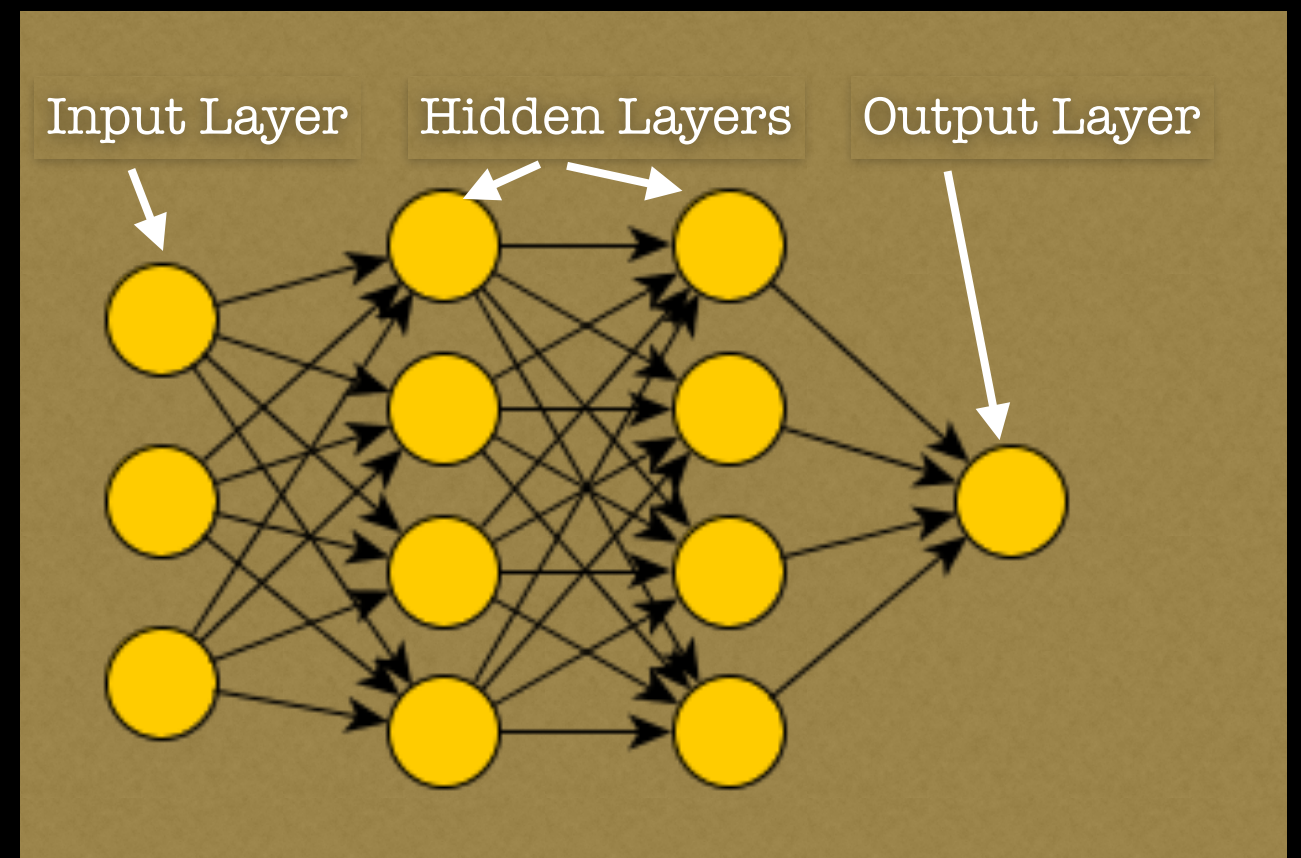
Specific operator which produces it

Broad Categories of ML

- ◆ Supervised Learning (labelled data)
- ◆ Unsupervised Learning (finding patterns and structure)
- ◆ Reinforcement Learning (interaction with an environment)

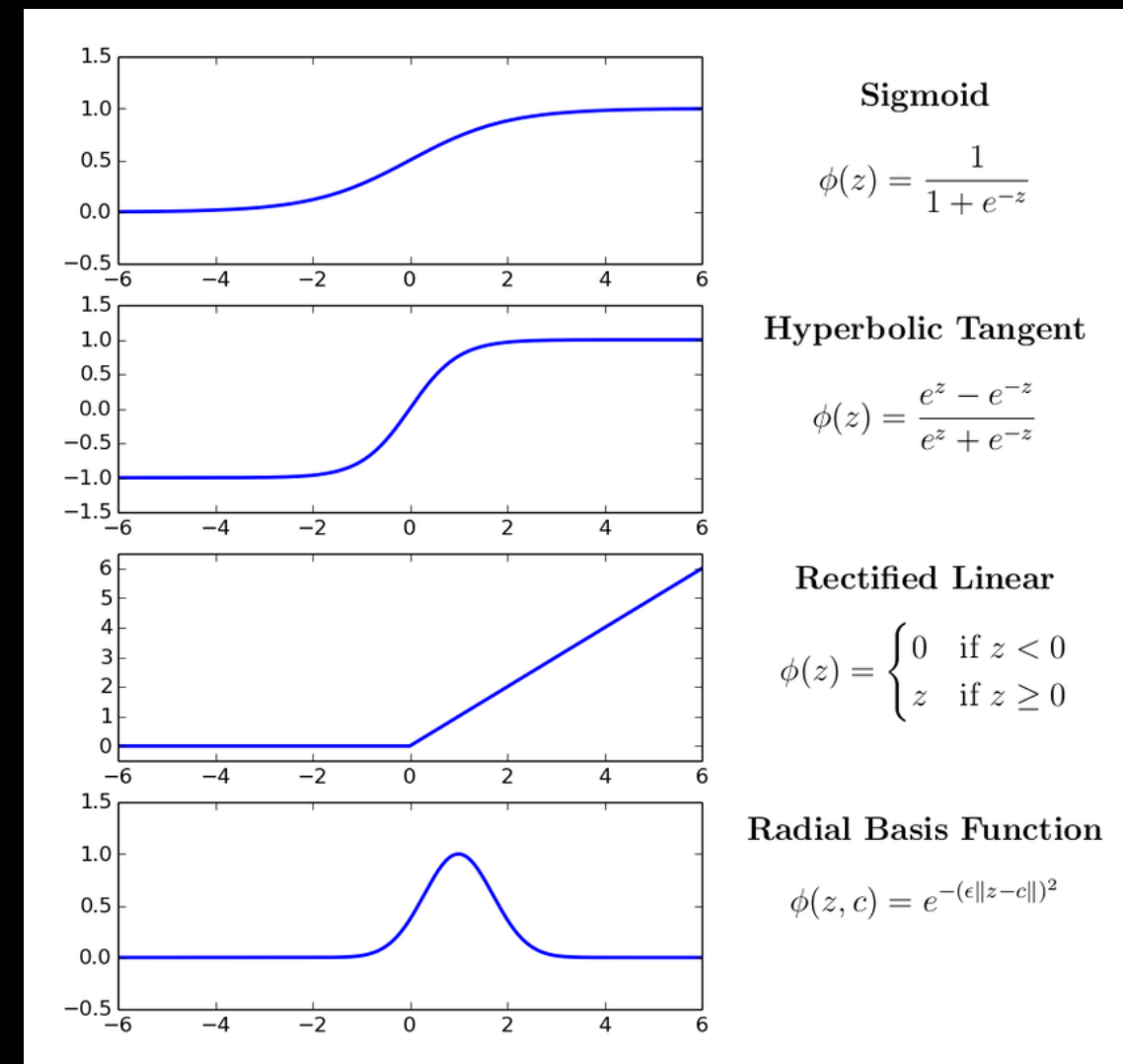
Neural Network : basic structure

- ◆ Input layer nodes : set of observables(kinematical features)
- ◆ Number of hidden layers (shallow or deep NN)
- ◆ Output layer : binary/multi-class classification

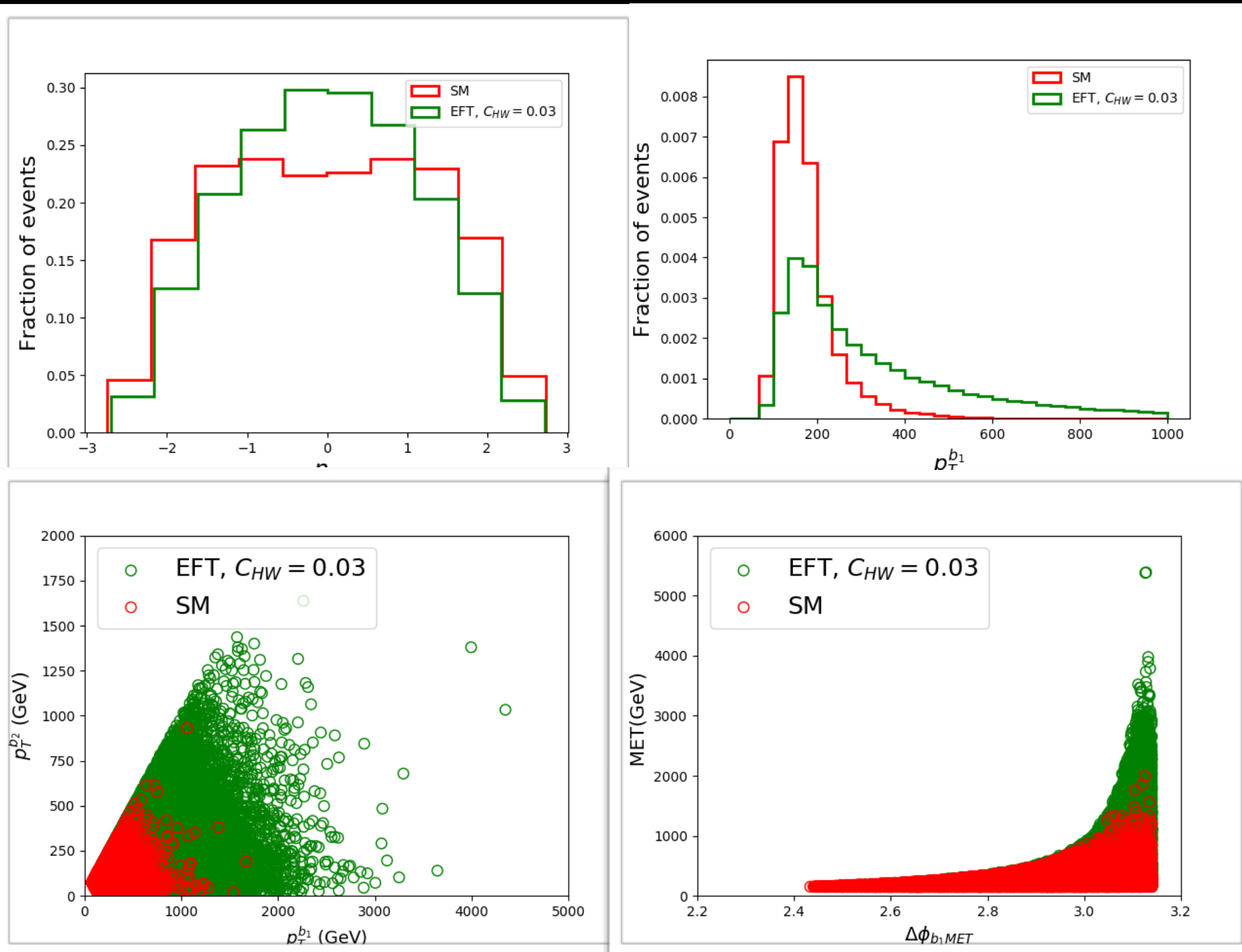


Key Insights

- ◆ Loss function
- ◆ Dropouts
- ◆ Activation function
- ◆ Backpropagation
- ◆ Epochs
- ◆ Receiver operative characteristic (ROC)



1D and 2D features



Appropriate Performance Measure for HEP Analysis

Discovery Significance $\frac{s}{\sqrt{B}}$

Asimov Significance

$$Z_A = \left[2 \left((s+b) \ln \left[\frac{(s+b)(b+\sigma_b^2)}{b^2 + (s+b)\sigma_b^2} \right] - \frac{b^2}{\sigma_b^2} \ln \left[1 + \frac{\sigma_b^2 s}{b(b+\sigma_b^2)} \right] \right) \right]^{1/2}$$

Specific (Asimov) Loss function

$$\ell_{s/\sqrt{s+b}} = (s+b)/s^2$$

Glen Cowan, Kyle Cranmer, Eilam Gross, Ofer Vitells, arXiv:1007.1727[physics.data-an]

Adam Elwood and Dirk Krücker, arXiv: 1806.00322[hep-ex]

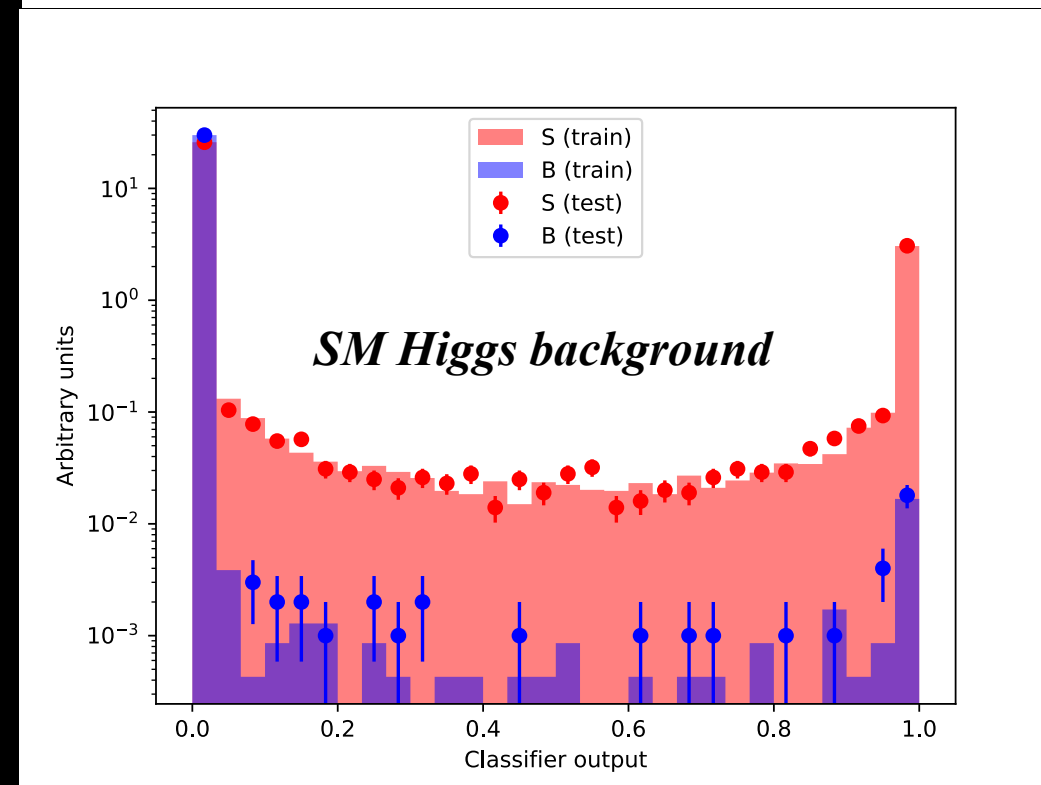
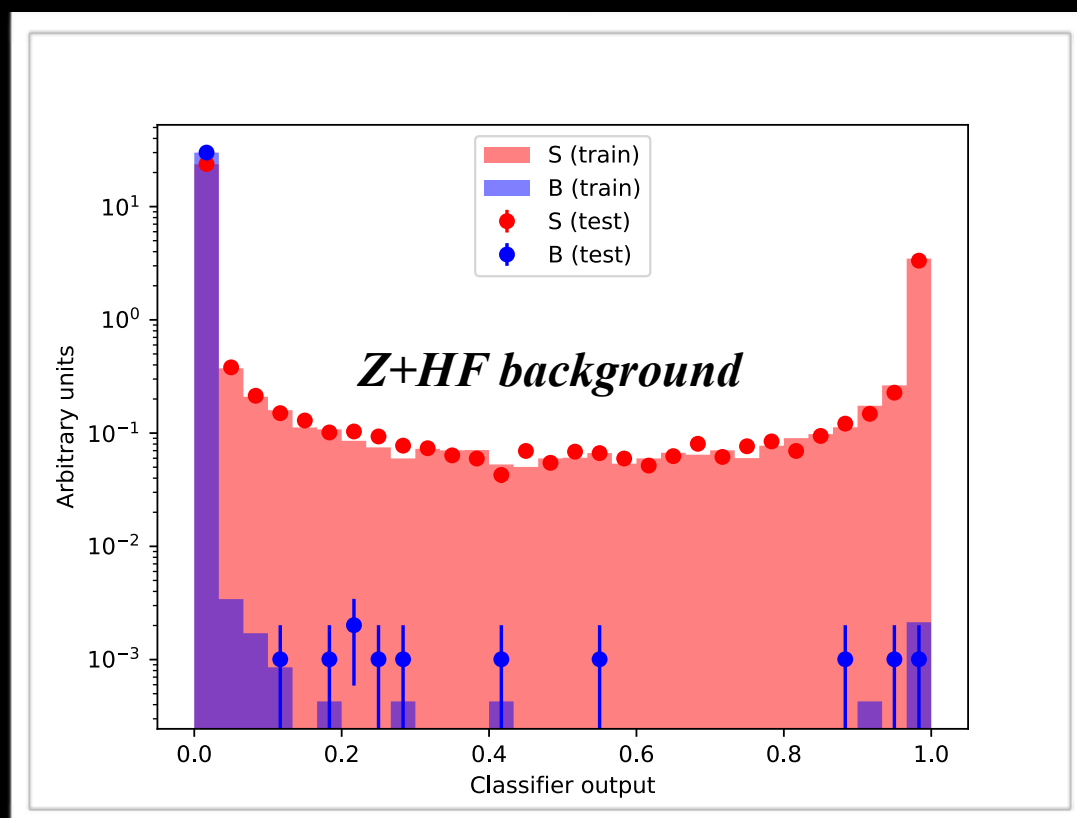
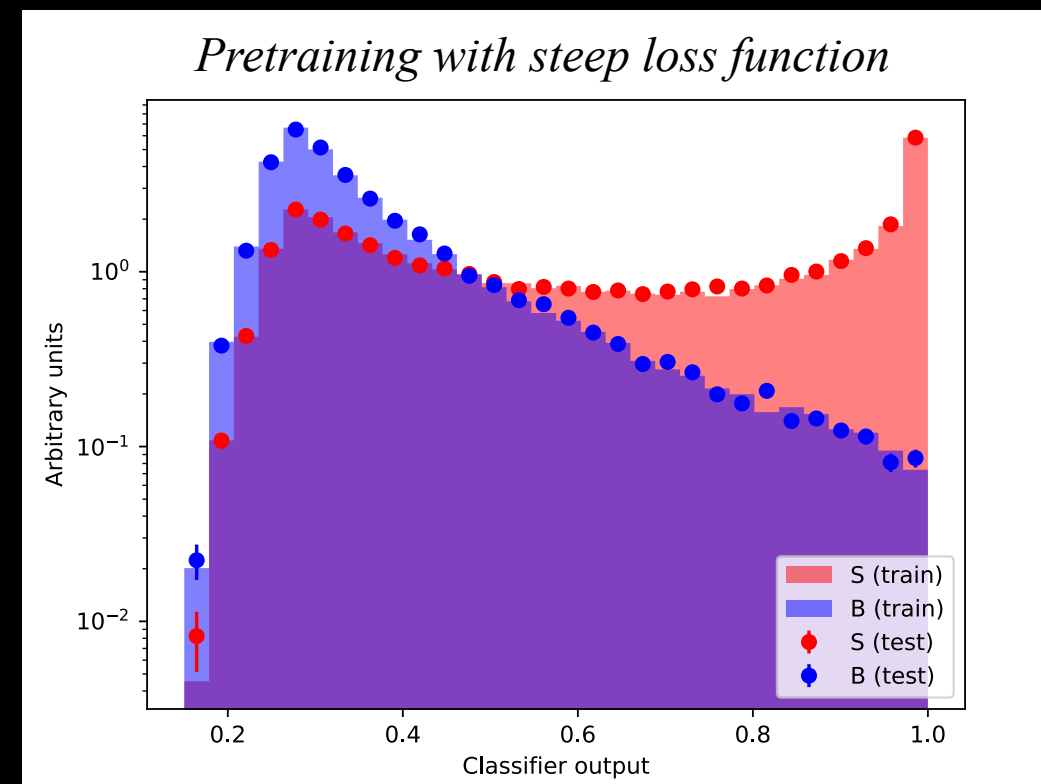
Neural Network Architecture

- ◆ Hidden layer : 1 (optimised)
- ◆ Dropouts : 0.2
- ◆ Activation function : ReLu
- ◆ Training set : Test set = 70 % : 30% (data scaling)
- ◆ Loss function : Asimov loss function (pre-training with MSE)

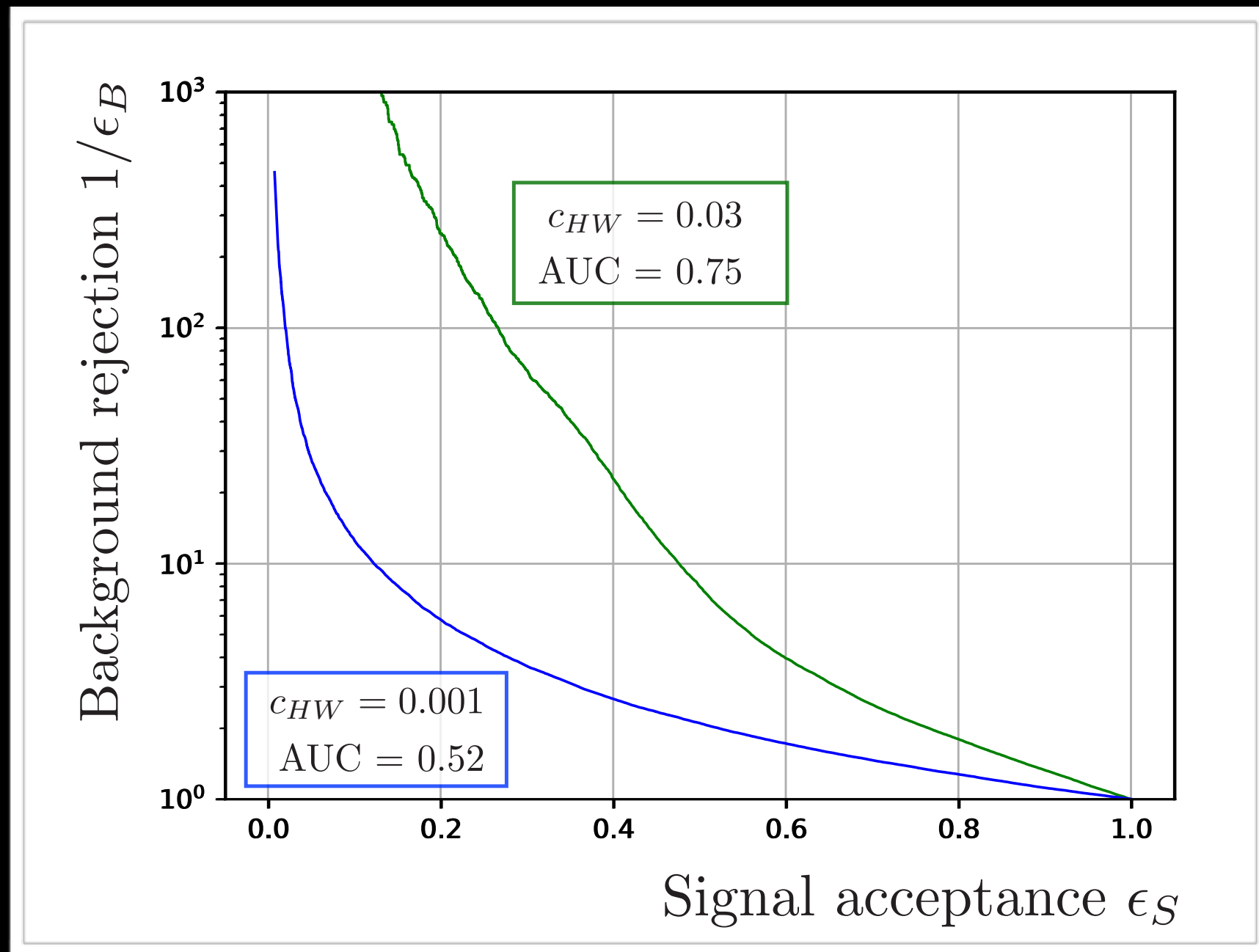
Classifier Output

Pre-training with usual loss function and
5 epochs

Final distributions with
Asimov loss function

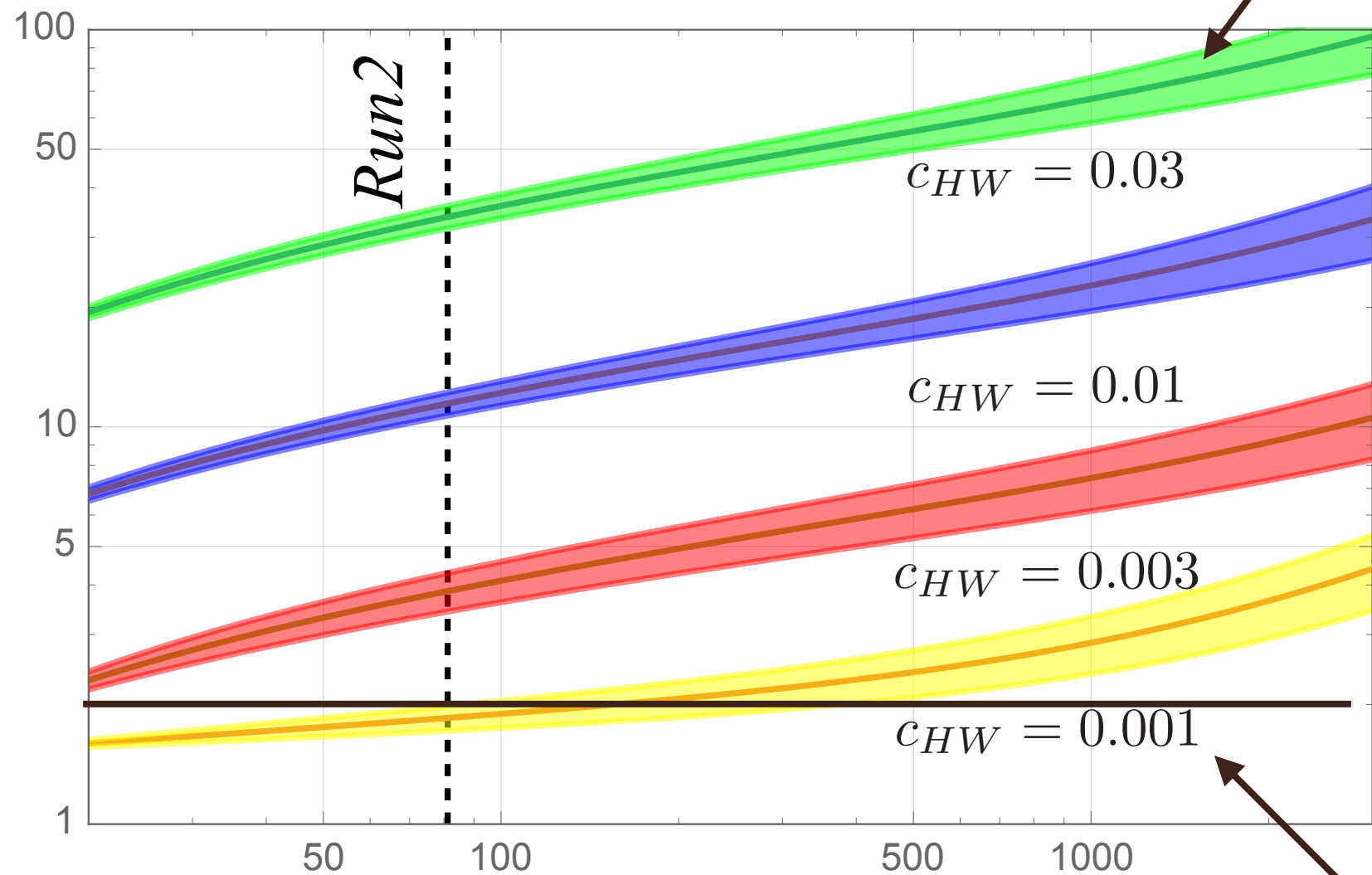


ROC (SMEFT vs SM Higgs background)



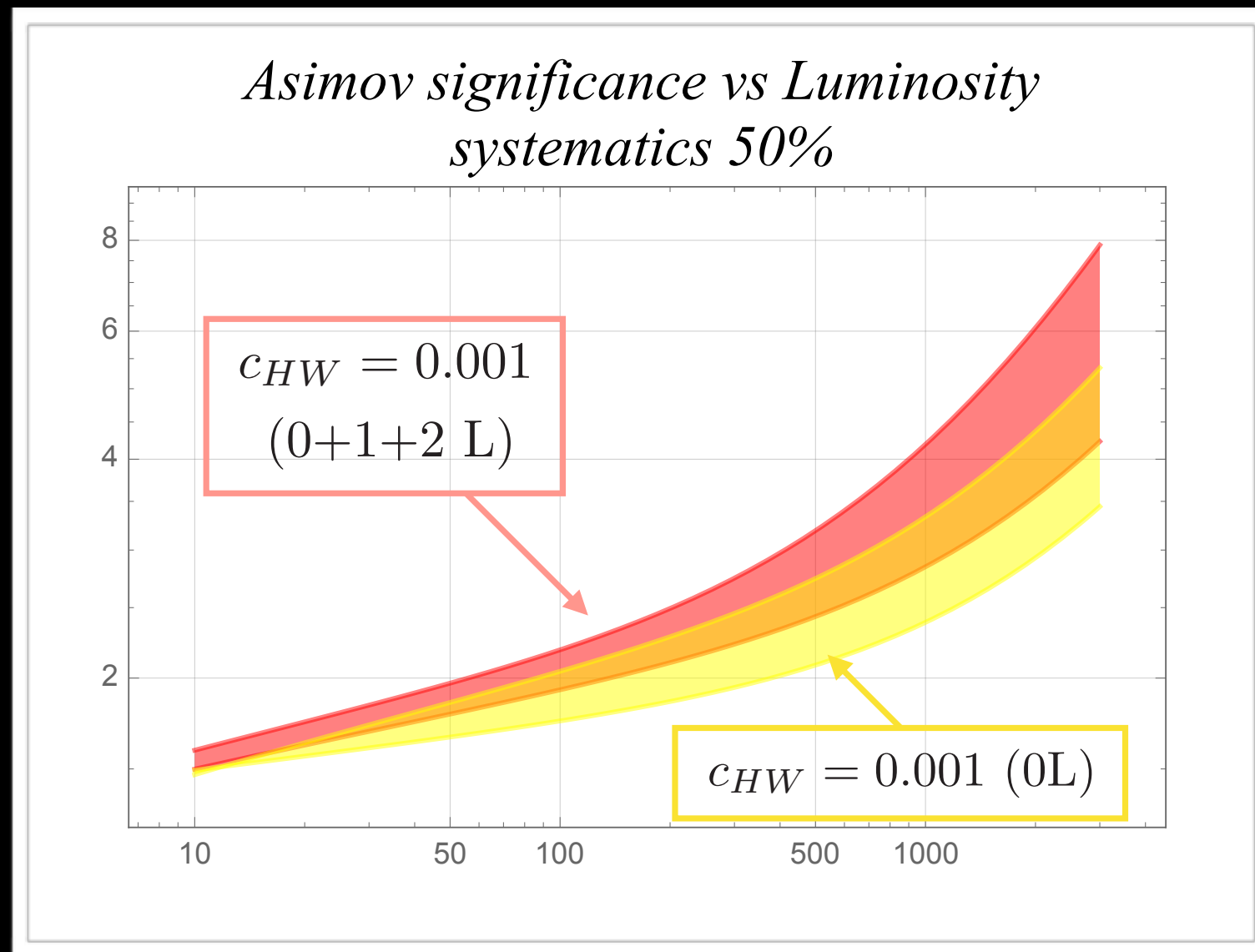
Current limit at 95% CL

*Asimov significance vs Luminosity
systematics 50%*



Possible improvement

Combining 0L+1L+2L for a limiting case



But for a realistic analysis combining different channels may help!!

Further ...

- ◆ This analysis is a “proof-of-concept” analysis
- ◆ Scaling for more operators and coefficients
- ◆ Hadronization, showering effects, detector simulation
- ◆ Global analysis using this algorithm (is in progress)
- ◆ We are discussing with ATLAS (VH) subgroup
- ◆ Different algorithms for same analysis set-up

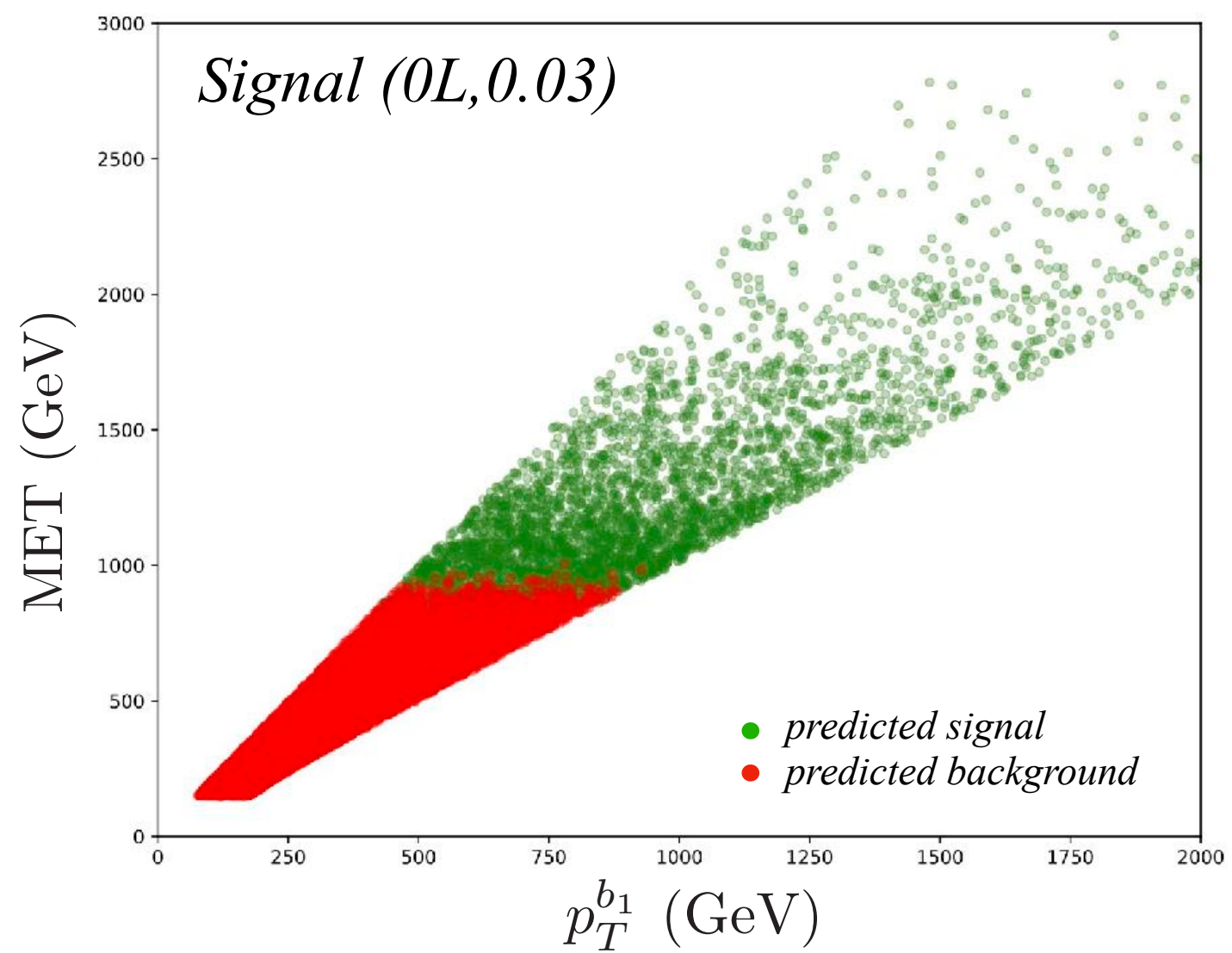
Summary and Outlook

- ◆ Use of ML techniques to exploit kinematic information in SMEFT framework
- ◆ VH channel analysis (proof-of-concept) : one operator
- ◆ This analysis may provide significant stronger bounds on EFT coefficient
- ◆ Scalability for more operators
- ◆ Use/test this approach for actual LHC data

A visualization of a cosmic web, showing a dense network of white filaments against a black background. A large, semi-transparent blue sphere is centered on a bright yellow point where many yellow lines converge. Green rectangular markers are scattered along the filaments and near the central point. Blue rectangular markers are visible in the upper left corner.

Thanks

Questions ?



Bias-Variance Trade-off

Bias : Deviation from the true value

Variance : fluctuations due to sample size

