

Flavour anomalies: a model building perspective

Marzia Bordone Universität Siegen

> QMLU 14.11.2019

Introduction

The Standard Model

The theory that describes with success the interactions between elementary particle is the Standard Model.

- 12 gauge bosons which mediate strong and electroweak interactions between elementary particles
- 3 generations of fermions characterised by the same quantum numbers
- a scalar field, the Higgs, which spontaneously breaks electroweak symmetry



Gauge vs Higgs sector

$$\mathcal{L}_{\mathsf{SM}} = \mathcal{L}_{\mathsf{gauge}} + \mathcal{L}_{\mathsf{higgs}}$$

$$\mathcal{L}_{\mathsf{SM}} = \boldsymbol{\mathcal{L}}_{\mathsf{gauge}} + \mathcal{L}_{\mathsf{higgs}}$$

Gauge Sector:

- completely specified by the gauge symmetry and the transformation properties under it of elementary particles
- interactions between gauge bosons and fermions are universal
- completely degeneracy of the three families

$$\mathcal{L}_{\mathsf{SM}} = \mathcal{L}_{\mathsf{gauge}} + \mathcal{L}_{\mathsf{higgs}}$$

Gauge Sector:

- completely specified by the gauge symmetry and the transformation properties under it of elementary particles
- interactions between gauge bosons and fermions are universal
- completely degeneracy of the three families

Higgs Sector:

- breaks arbitrarily the degeneracy of the three families
- when EWSB happens, it contains mass terms for quarks and leptons

$$-\mathcal{L}_{\mathrm{higgs}} \supset Y^{ij}_d \bar{Q}^i_L H d^j_R + Y^{ij}_u \bar{Q}^i_L H^c u^j_R + Y^{ij}_e \bar{L}^i_L H e^j_R$$

The flavour structure

The structure of the Yukawa matrices in the quark sector is rather peculiar



When we diagonalise the Yukawa matrices, we find that the flavour sector is completely specified by

- 6 eigenvalues of the quark Yukawa matrices + 3 for charged leptons
- the CKM mixing matrix of the quark sector, which is completely specified by 4 parameters
- these parameters are very well measured



The flavour problem

Open questions:

- Why does the flavour sector have such a peculiar structure?
 ⇒ flavour problem
- Is there something else which distinguish the three generations? \Rightarrow NP flavour problem

The flavour problem

Open questions:

- Why does the flavour sector have such a peculiar structure?
 ⇒ flavour problem
- Is there something else which distinguish the three generations? \Rightarrow NP flavour problem

It is flavour physics the research sector which addresses such open issues. The goal of flavour physics is investigating the **nature** and **structure** of the interactions between particle of different families in order to identify

The flavour problem

Open questions:

- Why does the flavour sector have such a peculiar structure?
 ⇒ flavour problem
- Is there something else which distinguish the three generations? \Rightarrow NP flavour problem

It is flavour physics the research sector which addresses such open issues. The goal of flavour physics is investigating the **nature** and **structure** of the interactions between particle of different families in order to identify

- possible NP scenarios at high energies which may lead to the pattern we measure at the SM scale
- NP contribution may be suppressed by their typical energy scale ⇒ we can probe processes and scale beyond the reach of direct searches



Recently, Babar, Belle and LHCb provided interesting results in *B*-physics.

They see a few hints of Lepton Flavour Universality Violation: channels with different lepton species in the final state behave differently

The channels explored so far are semileptonic decays of B-meson

- Flavour changing neutral currents b
 ightarrow s: μ vs e
- Charged currents b
 ightarrow c: au vs μ/e

$b \rightarrow c$ semileptonic transitions

Tree-level process within the SM

Effective hamiltonian description

$$\mathcal{H}_{\text{eff}} = -\frac{4G_F}{\sqrt{2}} V_{cb} \left(\bar{c}_L \gamma_\mu b_L \right) \left(\bar{\tau}_L \gamma_\mu \nu_L \right)$$

• Clean observables: careful treatment of m_{τ} dependent terms

$$R_{D^{(*)}} = \frac{\mathcal{B}(B \to D^{(*)}\tau\bar{\nu}_{\tau})}{\mathcal{B}(B \to D^{(*)}\ell\bar{\nu}_{\ell})}$$

- Deviation of $\sim 10\%$ -15% with respect to the SM predictions
- Combined significance $\sim 3.1\sigma$





$b \rightarrow s$ semileptonic transitions

Induced at loop level in the SM

Effective Hamiltonian description

$$\mathcal{H}_{\mathsf{eff}} = -4 \frac{G_F}{\sqrt{2}} V_{tb} V_{ts}^* \left[\dots + C_9 \mathcal{O}_9 + C_{10} \mathcal{O}_{10} \right]$$

 $\mathcal{O}_{9} = (\bar{s}\gamma^{\mu}P_{L}b) (\bar{\ell}\gamma_{\mu}\ell)$ $\mathcal{O}_{10} = (\bar{s}\gamma^{\mu}P_{L}b) (\bar{\ell}\gamma_{\mu}\gamma_{5}\ell)$

• Lepton Flavour Universality ratios

$$R_{K^{(*)}} = \frac{\mathcal{B}(B \to K^{(*)} \mu^+ \mu^-)}{\mathcal{B}(B \to K^{(*)} e^+ e^-)} \sim 2.1-2.6\sigma$$

• Angular Observables in $B \to K^* \mu^+ \mu^-$

$$P_5' = \frac{S_5}{\sqrt{F_L(1 - F_L)}} \quad \sim 3\sigma$$





 $\Delta C_9 \neq 0$ $\Delta C_{10} \neq 0$

Approach to the anomalies

SM predictions:

- investigate SM predictions for the observables of interest
- provide prediction for new channels/observables to get complementary informations

Model building:

• the effective scale of NP which could explain FCNC and CC anomalies is rather different

$$\Lambda \sim egin{cases} {
m few} imes {
m TeV} & {
m for} \ {
m CC} \ {
m few} imes {
m 10} \ {
m TeV} & {
m for} \ {
m FCNC} \end{cases}$$

• from EFT analysis we see that

[MB, Isidori, Trifinopoulos Buttazzo,Greljo,Isidori,Marzocca]

- FCNC and CC anomalies are addressed as a coherent pattern where NP is mainly coupled to the 3rd generation
- a flavour symmetry is required to suppress the couplings with light generations and provides a link to the Yukawa couplings

Non-trivial flavour structure needed

Are these signals of NP?

- After the analyses of 2019 we still don't see a clear sign of New Physics.
- Data will (eventually) lead us to a clear conclusion:
 - LHCb still has a large amount of data to be analysed for $b \to s \ell \ell$
 - Update of ${\cal R}_{{\cal K}^{(*)}}$ most likely to be ready in one year time
 - An update for R_{D^*} from LHCb is also due
 - New observables like $R(\Lambda_c)$ should be (soon) released
 - Belle II is taking data
 - Both ATLAS and CMS are building an interesting *B*-physics program

We need to keep looking

From the EFT to UV complete models

- EFT approach allows for a model independent combined analysis of the anomalies
- The leading NP must couple mainly to the 3rd generation of quarks and leptons
- A flavour symmetry suppresses and controls the couplings between NP and light generations: an interesting choice is U(2) flavour symmetry

 $U(2)^n$ flavour symmetry provides natural link to the Yukawa couplings.

Main idea: 3rd generation of fermions are complete singlets under $U(2)^n$ while the light generation have non trivial transformation properties under $U(2)^n$.



[Barbieri, Isidori, Jones-Perez, Lodone, Straub, '11]

The same symmetry-breaking pattern control the mixing 3rd -1st, 2nd generation for the NP responsible for the anomalies.

A good fit with data is obtained if $|V| \sim |V_{ts}| \sim 0.04$ and $\Delta \sim y_c \sim 0.006$.

U(2) correlations: FCNC

Working with flavour symmetries allows us to predict possible correlations between observables.

	$\mu\mu~(ee)$	au au	עע	$ au\mu$	μe
$m{b} ightarrow m{s}$	$R_{K^{(*)}}$	$B \to K^{(*)} \tau \tau$	$B \to K^{(*)} \nu \nu$	$B \to K \tau \mu$	$B \to K \mu e$
	$B_d o \mu \mu$	$B o \pi au au$	$B \to \pi \nu \nu$	$B o \pi au \mu$	$B \to \pi \mu e$
$m{b} ightarrow m{d}$	$B o \pi \mu \mu$				
	$B_s \to \bar{K}^{*0} \mu \mu$				
$oldsymbol{s} ightarrow oldsymbol{d}$			$K \to \pi \nu \nu$		$K ightarrow \mu e$

- $R_{K^{(*)}} = R_{\pi}$
- $B \to K^{(*)} \tau \tau \sim \mathcal{O}(100) \times \text{SM}, \ B \to \pi \tau \tau \sim \mathcal{O}(100) \times \text{SM}$
- $B \to K^{(*)}\nu\nu \sim \mathcal{O}(1) \times \mathsf{SM}, \ B \to \pi\nu\nu \sim \mathcal{O}(1) \times \mathsf{SM}, \ K \to \pi\nu\nu \sim \mathcal{O}(1) \times \mathsf{SM}$
- non-zero contribution to LFV processes

- NP only in left-handed operators.
- The leading NP effects arise in the 3rd generation of quarks and leptons only.
- The couplings to light generations are controlled by a $U(2)_q \times U(2)_\ell$, softly broken by two leading spurions V_q and V_ℓ for the quarks and the leptons sector, respectively.

$$egin{aligned} q_{3L} &\sim (\mathbf{1},\mathbf{1}) & \ell_{3L} &\sim (\mathbf{1},\mathbf{1}) \ Q_L &= (Q_L^1,Q_L^2) &\sim (ar{\mathbf{2}},\mathbf{1}) & L_L &= (\ell_L^1,\ell_L^2) &\sim (\mathbf{1},ar{\mathbf{2}}) \ V_q &\sim (\mathbf{2},\mathbf{1}) & V_\ell &\sim (\mathbf{1},\mathbf{2}) \end{aligned}$$

The framework



- Neglecting mixing with first generation, the parameters needed are 4: C_T , C_S , λ_{bs} , $\lambda_{\mu\mu}$.
- Fitting the CKM and Yukawa, we know that $\lambda_{bs} \sim \mathcal{O}(V_{cb})$.

Single particle solution

- Based on $U(2)^n$ flavour symmetry
- No contradiction between LFU anomalies and constraints from EWPT, flavour observables or hight-p_T data
- Possible one particle solution:

	Singlet	Triplet
Scalar LQ:	S_1	S_3
Vector LQ:	U_1	U_3
Colorless vector:	B'	W'

• The most promising single-mediator solution is the vector leptoquark $U_{\mu}\sim(3,1)_{2/3}$

UV completion needed



A UV completion for $U_{\mu} \sim (3,1)_{2/3}$

Two possibilities:

- Mediator of a composite state of a new strongly interacting sector
- Massive gauge boson of a spontaneously broken gauge theory

[Di Luzio, Grejlo, Nardecchia; Blanke, Crivellin; Fornal, Gadam, Grinstein; Di Luzio, Fuentes-Martín, Grejlo, Nardecchia, Renner]

The natural choice: Pati-Salam group \Rightarrow PS \equiv $SU(4) \times SU(2)_L \times SU(2)_R$

[Pati,Salam, Phys. Rev. D 10 (1974) 275]

- Quarks and leptons are part of the same multiplet of SU(4) ⇒ lepton are seen as the 4th colour
- No proton decay

 $\Psi_L = \begin{pmatrix} Q_L^{\alpha} \\ Q_L^{\beta} \\ Q_L^{\gamma} \\ L_L \end{pmatrix}$

Main problems:

- the LQ coupling with the heavy and light generations is flavour blind
- tights constrains in processes as $K_L \rightarrow \mu e \Rightarrow LQ$ mass $\sim 100 \,\mathrm{TeV}$

The "4321" model



At low energies we have:

- the SM
- the LQ U_1 with a mass $\mathcal{O}(1 \text{ TeV})$
- inevitably a massive color octect G' and a Z' with masses of $\mathcal{O}(1 \text{ TeV})$

The PS leptoquark introduces always new states

[Di Luzio, Greljo,Nardecchia, '17; Di Luzio, Fuentes-Martín, Greljo, Nardecchia, Renner, '18]

- The SM particles are charged only under the 321 component
- New vector-like are charged under the SU(4)

• The mixing between the vector-like and the SM fields induces effective SM-U₁ couplings



- The effective interactions between the SM fields and U_1 are mainly left-handed
- Using the freedom on the vector-like couplings it's possible to have a good fit to low energy data and avoid most of the constraints

A three-site model

Main Idea: at high energies the 3 families are charged under 3 independent gauge groups

 $\mathsf{PS}^3 = \mathsf{PS}_1 \times \mathsf{PS}_2 \times \mathsf{PS}_3$

- The breaking controls the hierarchy of the Yukawa couplings
- Low energy pheno is governed by the $\mathcal{O}(\text{TeV})$ breaking only
- At low scale we recover the SM + 1 LQ + 1 Z' and a coloron
- The LQ couples to both LH and RH fermions



A three-site model

Main Idea: at high energies the 3 families are charged under 3 independent gauge groups

 $\mathsf{PS}^3 = \mathsf{PS}_1 \times \mathsf{PS}_2 \times \mathsf{PS}_3$

- The breaking controls the hierarchy of the Yukawa couplings
- Low energy pheno is governed by the $\mathcal{O}(\text{TeV})$ breaking only
- At low scale we recover the SM + 1 LQ + 1 Z^\prime and a coloron
- The LQ couples to both LH and RH fermions



Fit to low energy data



- Good fit to low energy data within the 1σ region
- RH currents help to ease the tension with $R_{D^{(\ast)}}$ and rise the NP scale

[MB, Cornella, Fuentes-Martín, Isidori, '17, '18]

[Cornella, Fuentes-Martín, Isidori, '19]



- RH currents generate interesting contributions in *B_s* decays
- LFV processes are a smoking gun of this model

High- p_T constraints on PS models

- The most stringent bound on U_1 comes from $pp \to \tau \tau$
- The bound on Z' are weaker
- Bounds on G' come from $pp \to \bar{t}t$ but it becomes weaker as the width increases
- The relation between M_U and $M_{G'}$ in PS³ helps to create combined exclusion limits



[Baker, Fuentes-Martín, Isidori, König, '19]



 $g_U \sim 3 \Rightarrow M_U \geqslant 3.8 \, \text{GeV}$

A Froggatt-Nielsen based idea

- The main goal of FN mechanism is to explain the mass hierarchies between quarks
- The main point is enlarging the gauge group adding an additional U(1) and extra heavy fermions
- The SM fermions are charged under the $U(1),\,{\rm and}$ the charges are generation dependent
- The U(1) is spontaneously broken by a new scalar field $\phi_{\rm FN}$
- The Yukawa scale as the parameter $\lambda = \langle \phi_{FN}
 angle / \Lambda_{FN} \ll 1$

SM fields charges

According to the assignment of charges of the SM fields, we have:

$$\begin{split} (Y_U)_{ij} &\sim \lambda^{|b_Q^i - b_U^j|} \\ (Y_D)_{ij} &\sim \lambda^{|b_Q^i - b_D^j|} \\ (Y_E)_{ij} &\sim \lambda^{|b_L^i - b_E^j|} \end{split}$$

In order to reproduce the CKM

$$(V_{\mathsf{CKM}})_{ij} = (Y_U^{\dagger} Y_D)_{ij} \sim \lambda^{|b_Q^i - b_Q^j|} \qquad \lambda = \sin^2 \theta_c \sim 0.2$$

There is no first principle which determines the FN charges.

Quarks

- CKM \Rightarrow set the charges of the left-handed doublets
- quark masses \Rightarrow we reduce the number of possible charges to two values for each right-handed quark

Lepton

• lepton masses masses ⇒ constraining only differences of left-handed and right-handed charges

More pheno constraints are needed

- Using low energy pheno implies choosing a particular set of spurions to describe data
- This affects heavily the choices for lepton charges
- A driving role is played by B anomalies

A U_1 simplified model

No UV completion discussed, interactions with fermion only:

$$\mathcal{L}_{U_1} = \Delta_{QL}^{i\alpha} \bar{Q}^i \gamma_{\mu} L^{\alpha} U_1^{\mu} + \Delta_{DE}^{i\alpha} \bar{d}_R^i \gamma_{\mu} e_R^{\alpha} U_1^{\mu} + \text{h.c.}$$

$$\uparrow \\ c_{QL}^{i\alpha} \lambda^{|b_Q^i - b_L^{\alpha}|} c_{DE}^{i\alpha} \lambda^{|b_D^i - b_E^{\alpha}|}$$

$$\begin{split} \mathcal{L}_{\text{eff}} &= \mathcal{L}_{\text{SM}} - \frac{1}{\Lambda^2} \bigg\{ [\mathcal{C}_{lq}^{(3)}]^{ij\alpha\beta} (\bar{Q}^i \gamma^\mu \sigma^a Q^j) (\bar{L}^\alpha \gamma_\mu \sigma^a L^\beta) + [\mathcal{C}_{lq}^{(1)}]^{ij\alpha\beta} (\bar{Q}^i \gamma^\mu Q^j) (\bar{L}^\alpha \gamma_\mu L^\beta) \\ &+ [\mathcal{C}_{ed}]^{ij\alpha\beta} (\bar{d}^i_R \gamma^\mu d^j_R) (\bar{e}^\alpha_R \gamma_\mu e^\beta_R) + [\mathcal{C}_{ledq}]^{ij\alpha\beta} (\bar{Q}^i_L d^j_R) (\bar{e}^\alpha_R L^\beta) + \text{h.c.} \bigg\} \,, \end{split}$$

Tree-level matching

$$\begin{split} [\mathcal{C}_{lq}^{(1)}]^{ij\alpha\beta} &= [\mathcal{C}_{lq}^{(3)}]^{ij\alpha\beta} = + \Delta_{QL}^{i\alpha} \Delta_{QL}^{*j\beta} \,, \\ [\mathcal{C}_{leqd}]^{ij\alpha\beta} &= -2 \, \Delta_{QL}^{i\alpha} \Delta_{DE}^{*j\beta} \,, \\ [\mathcal{C}_{ed}]^{ij\alpha\beta} &= + \Delta_{DE}^{i\alpha} \Delta_{DE}^{*j\beta} \,. \end{split}$$

Two step approach to study low energy phenomenology

- We determine the FN charges
 - We use the decays $Z \to \nu\nu$, $b \to s\mu^+\mu^-$, $b \to c\tau\bar{\nu}$, $B_d \to \tau^-\mu^+$, $B_s \to \tau^\pm\mu^\mp$, $K_L \to \mu^\pm e^\mp$ to select charges compatible with experimental limits
 - The combination of model dependent and independent constraints gives possible 24 scenarios.
- Fit to a larger set of observables for each of the 24 scenarios

Full fit to the allowed scenarios

• We parametrise the Wilson coefficients as

$$c_{QL}^{i\alpha} = \pm \mathcal{C}_{QL} \qquad c_{DE}^{i\alpha} = \pm \mathcal{C}_{DE}$$

The FN power counting is the only mechanism responsible of suppression/enhancement of the different flavour entries

• We choose the following to be able to fit phenomenology



• We set $\Lambda=2\,{\rm TeV}$

• Larger set of observables: LFV B decays, W LFU, universality in V_{cb} .

Fit results

Scenario	b_L^1	b_D^1	b_D^2	b_D^3	b_E^1	b_E^2	b_E^3	\mathcal{C}_{QL}	\mathcal{C}_{DE}
1a	-2	10	-3	-3	-11	4	-2	1.10 ± 0.07	0.72 ± 0.22
1b		10	$\overline{7}$	-3	-11	-6	-2	1.07 ± 0.08	6.4 ± 1.8
1c		10	$\overline{7}$	3	-11	-6	4	1.07 ± 0.08	7.2 ± 2.1
1d		-4	-3	-3	-11	4	-2	1.10 ± 0.09	0.74 ± 0.28
1e		-4	-3	-3	7	4	-2	1.10 ± 0.09	0.73 ± 0.28
2a		10	-3	-3	17	4	-2	1.10 ± 0.10	0.74 ± 0.26
2b	1.0	10	$\overline{7}$	-3	-1	-6	-2	1.09 ± 0.09	0.42 ± 0.25
2c		10	$\overline{7}$	-3	17	-6	-2	1.08 ± 0.09	4.6 ± 1.4
2d	+0	10	$\overline{7}$	3	-1	-6	4	1.07 ± 0.10	7.1 ± 2.0
2e		10	7	3	17	-6	4	1.08 ± 0.09	4.8 ± 1.3
2f		-4	-3	-3	17	4	-2	1.10 ± 0.09	0.74 ± 0.28

Common features:

- $b \rightarrow s \mu^+ \mu^-$ dominated by left-handed operator
- $b \rightarrow s e^+ e^-$ is negligible
- B_c life time is not spoiled

•
$$\Delta \chi^2 = \chi^2 |_{\text{SM}} - \chi^2 |_{\text{NP}} \sim 30$$



- High correlation between R_D and $\bar{B}_s \to \tau^+ \tau^-$ due to sizeable scalar contributions
- Better measurements of $\bar{B}_s\to \tau^+\tau^-$ provide a strong indication on the chirality of the NP operators in $R_{D^{(*)}}$

Fit results



- LFV B decays constitute an important signature of this scenarios
- For both the $\bar{B}_{d,s}$ modes, the final state with a τ^+ is enhanced with respect to final state with a τ^-
- Especially for the \bar{B}_s initial state, the predictions approach the current experimental limit

With scalars LQ, we need at least two mediators

- Composite scenario: S_1+S_3
 - Strong dynamics not known
 - B_s mixing + EWPT create tension with $R_{D(*)}$
 - Need to enforce some couplings to be zero to avoid proton decay
- GUT inspired scenarios: $S_3 + R_2$

[Bečiveríc, Doršner, Fajfer, Faroughy,Košnik,Sumensari]

- Predicts interesting LFV signals
- No explicit realisation so far which avoids proton decay

[D.Marzocca]

What is still to be done?

Model	$R_{K^{(\ast)}}$	$R_{D^{(\ast)}}$	$R_{K^{(*)}} \ \& \ R_{D^{(*)}}$
S_1	X *	 Image: A start of the start of	X *
R_2	X *	 Image: A second s	×
$\widetilde{R_2}$	×	×	×
S_3	 Image: A second s	×	×
U_1	 	 	✓
U_3	 ✓ 	×	×

- Colourless solution W' + Z': tension with high- p_T searches with $\tau_L \tau_L$ or $b_L b_L$ final states [Greljo,Isidori,Marzocca,'15]
- Solutions with right-handed neutrino are motivated and help to ease the tension with $b \to c \tau \nu$ data but they are most likely to be excluded from high- p_T

[Greljo, Camalich, Ruiz-Álvarez, '18]

It seems like there is not much space left...

...but data can help us!

If the anomalies are trues, NP must appear somewhere else.

A full dedicated flavour physics program run by LHCb, Belle II but also experiments like NA62 is needed to

- determine the flavour structure of the NP sector;
- different correlations among low energy observable can help to distinguish the possible models.

Only with such programs will we be able to determine what type of NP is realised in nature.

- Anomalies in *B*-physics are an interesting puzzle
- It is not clear yet if these are the first hints of NP
- BSM scenarios are viable and testable both in direct and indirect searches
 - The U_1 vector leptoquark seems to be the most favoured solution
 - A UV completion based on the Pati-Salam gauge group provides a combined explanation of LFU violation and the hierarchy of the Yukawa couplings
 - A new idea based on Froggatt-Nielsen mechanism gives viable results
 - All these scenario provide interesting signatures as LFV ${\cal B}$ decays